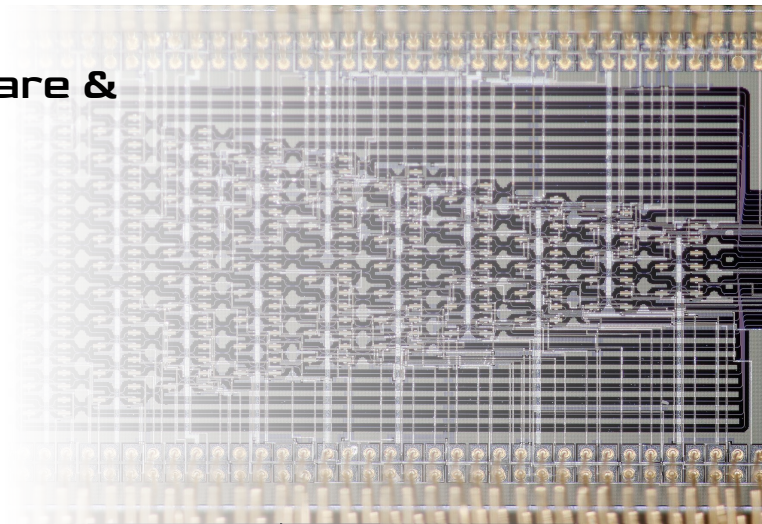




# Co-design of machine intelligence and hardware & the need for verifiable AI

MIT AI Hardware Program Symposium | 2025.11.12

Dirk Englund  $\in$  {RLE, MTL, EECS}@MIT



Quantum Computing & Networking

ML signal processing

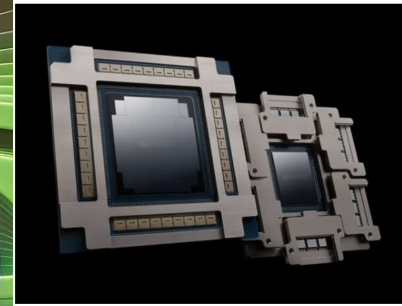
# A Renaissance in Specialized Computing

1. Quantum Computing
2. AI: perception, generative, agentic
3. Physical AI



Nvidia GTC, 2025

# Photonics at the forefront



## Nvidia looks to silicon photonics to cut datacentre AI power

Technology News | March 21, 2025

By Nick Flaherty

OPTOELECTRONICS

AI

POWER MANAGEMENT

Nvidia GTC, 2025

## Scalable qubit systems ( $10^3$ - $10^6$ )

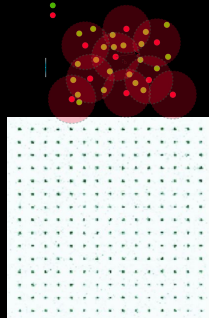
.. in solids



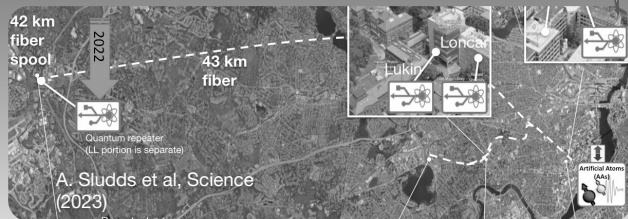
M Bhaskar et al, Nature 2020;  
N. Wan et al, Nature 2021; PRL  
2022, PRX 2022

10  $\mu$ m

.. or vacuum (with CUA: Vuletic,  
Greiner, Lukin)

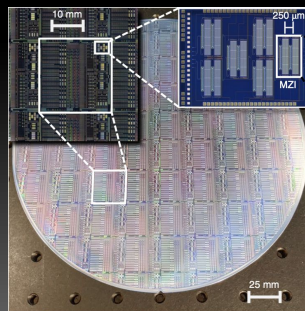


Full systems: quantum networks,  
AI, quantum sensors

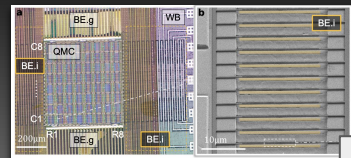


with Manya Ghobadi (CSAIL), MIT LL Grp 67, and Karl Berggren (EECS)

## Semiconductor devices



M Dong et al, Nature  
Photonics 2021



L Li et al (with Prof Ruonan  
Han)

## Theory & algorithms: physics, control theory, CS

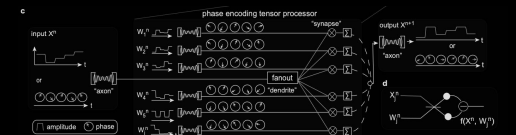
QPG-MIT



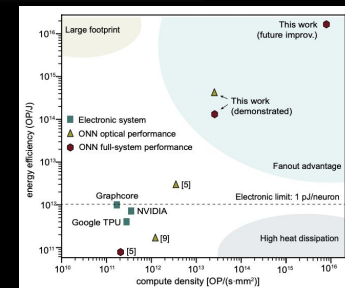
$$H = \frac{\hbar\Omega_{\mu\nu}}{2} \sum_l \sigma_x^l - \frac{\hbar\delta_{\mu\nu}}{2} \sum_l \sigma_z^l + \sum_{i \neq j} \frac{C_3}{R_{ij}^3} (\sigma_x^i \sigma_x^j + \sigma_y^i \sigma_y^j)$$



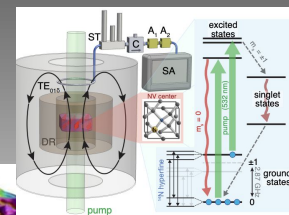
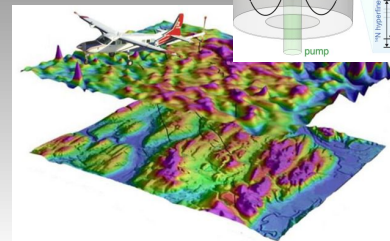
## AI / machine learning



Z. Chen, Nature  
Photonics  
(2023)

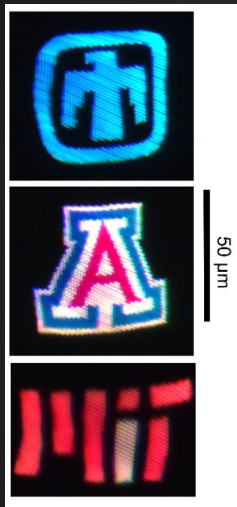
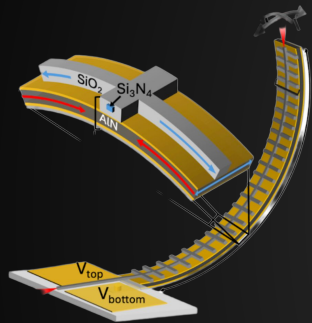


w. D Braje, MIT  
LL, M Trusheim  
MIT RLE & ARL





# PIC technology



M Saha, Y. Henry Wen, et al, arXiv <https://arxiv.org/abs/2406.17662> (2025)

See also  
M Dong et. al, Nature Photonics (2021)  
A Menssen et. al. Optica (2023)

- MIT-Sandia National Laboratory - MITRE - Harvard  
Separately: QuEra - SNL  
- Process pioneered by Matt Eichenfield et al at Sandia NL  
Spin-off company in the works on PIC displays & sensors - Interested ?

## 16-CH APIC lithium niobate on insulator<sup>3</sup>

MIT QP  $\nabla$  Csem

→ Lightium, Inc

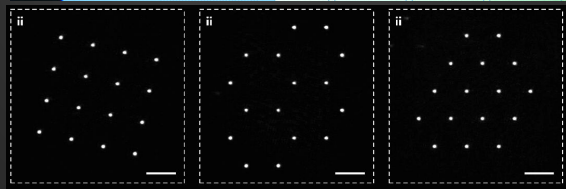
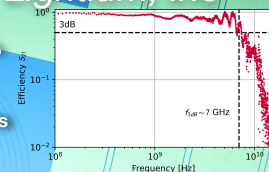
Mod rate > 5 GHz,

Pulse area error  $\sigma < 1\%$

Low voltage (<3V)

Scalable >> 16 channels

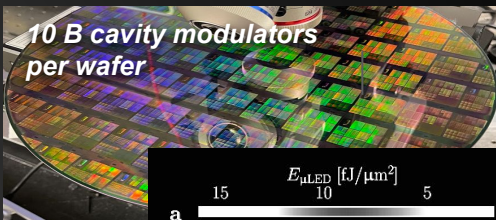
> 30 dB contrast



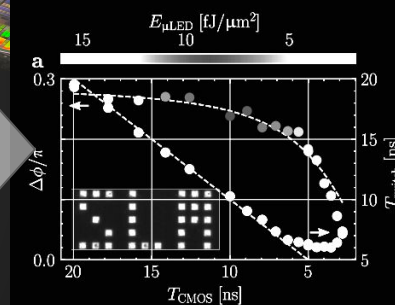
## 16 programmable beams, 10 GHz bandwidth

<sup>3</sup>I. Christen et al, Nature Comm (2025)  
H. Larocque, D. Vitullo, et al,

## 2D Spatial Light Modulator in Si demonstrator ( $v_{\text{mod}} \sim 1\text{GHz}$ )<sup>4</sup>



ns frames



<sup>4</sup>C. Panuski et al, Nature Photonics (2022)  
[CP awarded the 2022 Carl E. Anderson Division of Laser Science Dissertation Award]

48-ch EOMs ( $v_{\text{mod}} > 30\text{GHz}$ ):  
A. Sluuds et al, Science **378** (2022).

# Nanophotonic waveguide chip-to-world beam scanning at 68M Spots/s·mm<sup>2</sup>

Matt Saha<sup>\*1</sup>, Y. Henry Wen,<sup>\*1,2,α</sup> Andrew S. Greenspon<sup>\*1,2</sup>, Matthew Zimmermann<sup>\*1</sup>, Kevin J. Palm<sup>1,2</sup>, Alex Witte<sup>1</sup>, Yin Min Goh<sup>2</sup>, Chao Li<sup>2</sup>, Jonathan Bumstead<sup>3</sup>, Kevin Schädler<sup>4</sup>, Mark Dong<sup>1,2</sup>, Andrew J. Leenheer<sup>6</sup>, Genevieve Clark<sup>1,2</sup>, Gerald Gilbert<sup>5,‡</sup>, Matt Eichenfield<sup>6,7,&</sup>, and Dirk Englund<sup>2,4†</sup>

M Saha, Y. H. Wen, A. Greenspon, M. Zimmerman, et al,  
<https://arxiv.org/pdf/2406.17662>

The Scanning Waveguide Micro-Display  
for Augmented Reality

MITRE team,

PoC: Dr Henry Wen, MITRE

Henry Wen <[hwen@mitre.org](mailto:hwen@mitre.org)>

# The challenge:

3000  
nits

12hr  
batt

~1 cc  
~1 gram

4K ~8 MP

A bright, efficient, dime-sized, high-res display for each eye, in the frame of light-weight glasses



# Case study: Meta Orion

Most advanced research prototype

Result of >\$10B R&D

Not mass producible

>\$10,000 per unit cost

Large Field-of-View (70°) 👍

Low resolution (13 PPD→0.39 MPix) 👎

Low Brightness (400 nits→indoor only) 👎

Short battery (2-3hrs) 👎

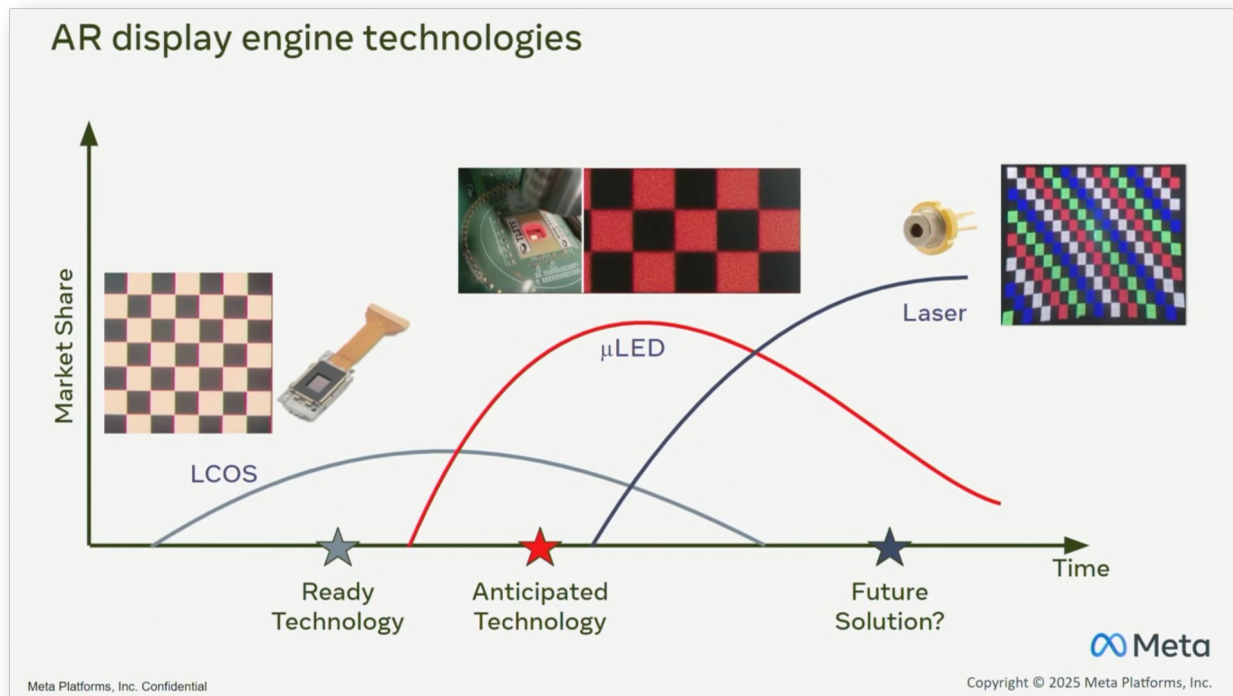
Requires: →8 MP for immersive

→3000 nits for outdoor





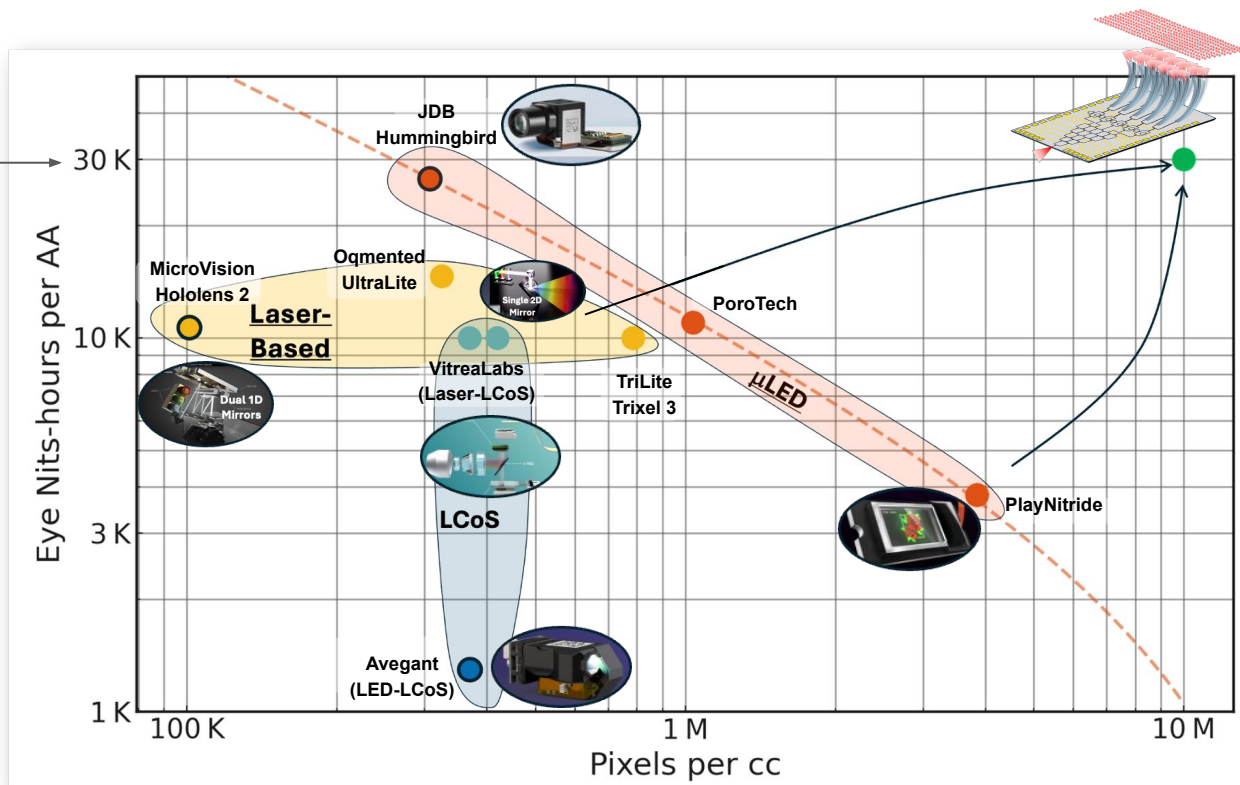
# Bright + efficient requires lasers



# State of art

10hrs @  
3000 nits

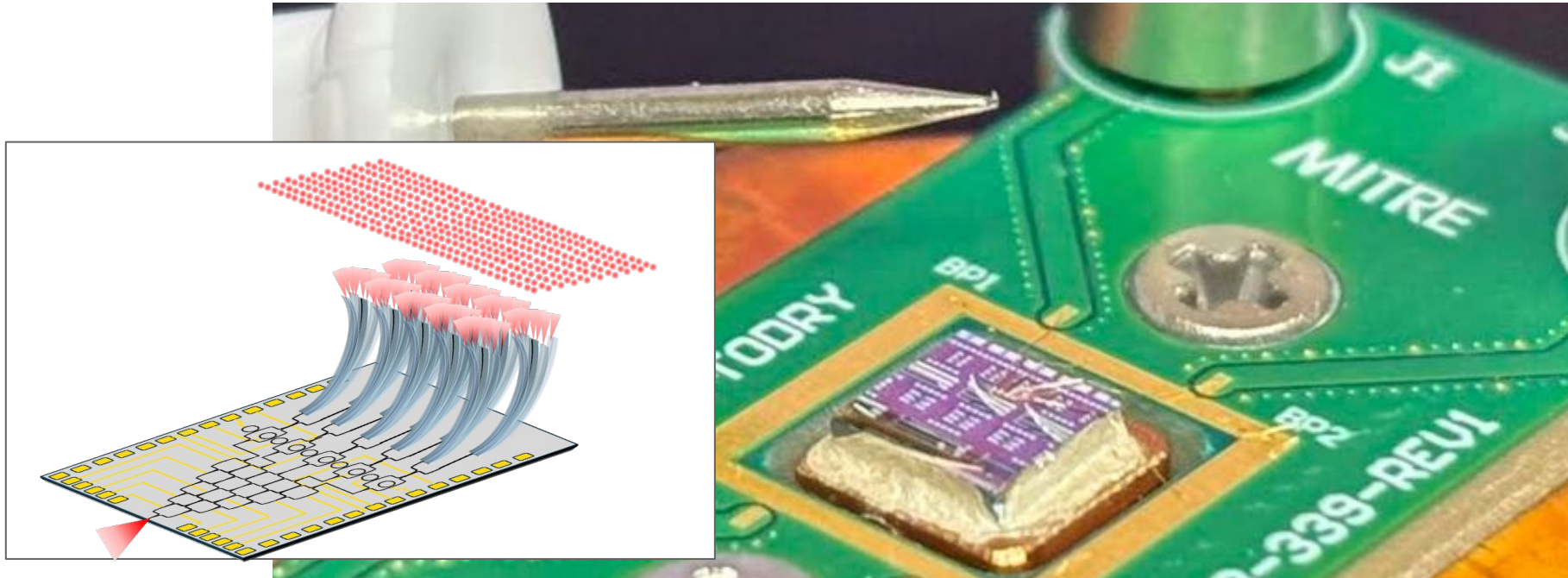
How bright and how  
long it can last



How many pixels for a given volume

# Nanoelectromechanical PIC display

18



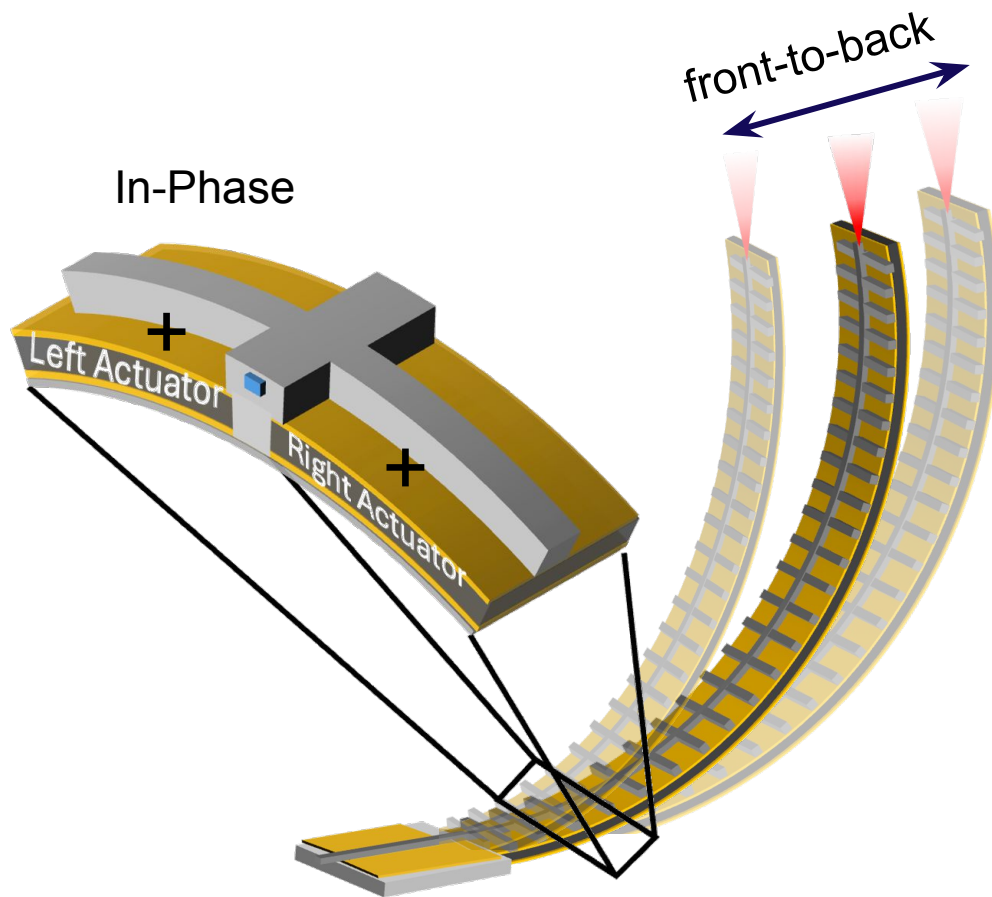
# Scan

Low voltage ( $<5V$ ) requirement enables CMOS compatibility

Scan frequency  $> 4$  KHz

$<1$   $\mu m$  pixel pitch

6.8M pixels per second per scanner





# Scan

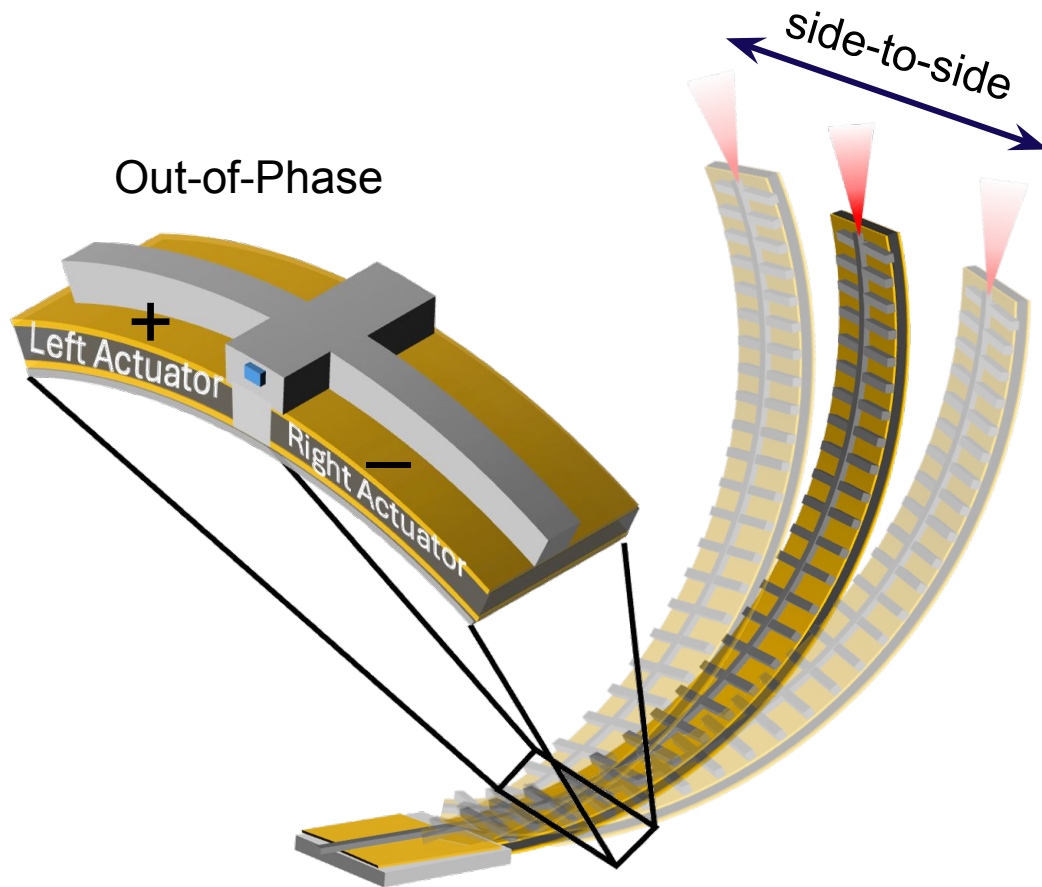
20

Low voltage (<5V) requirement enables CMOS compatibility

Scan frequency > 8 KHz

<1  $\mu\text{m}$  pixel pitch

6.8M pixels per second per scanner

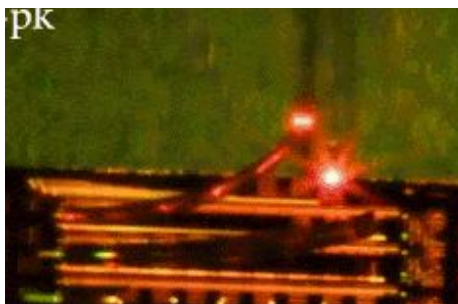


# TECH DEMONSTRATION

21

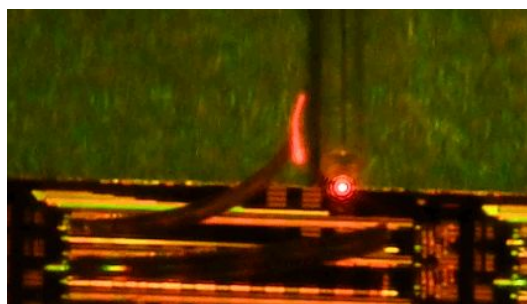
## 1 FRONT-BACK

Front-to-back movement



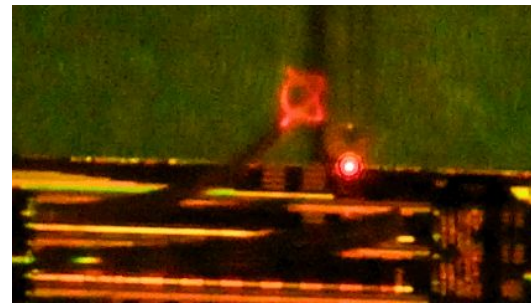
## 2 SIDE-TO-SIDE

Side-to-side movement



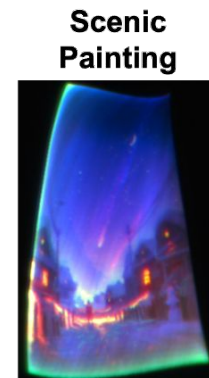
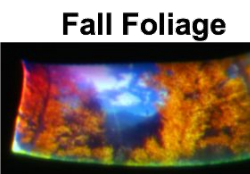
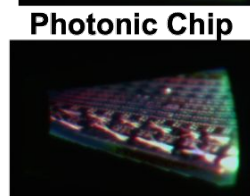
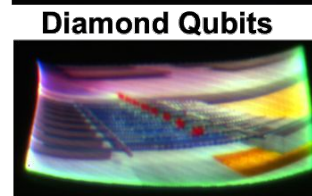
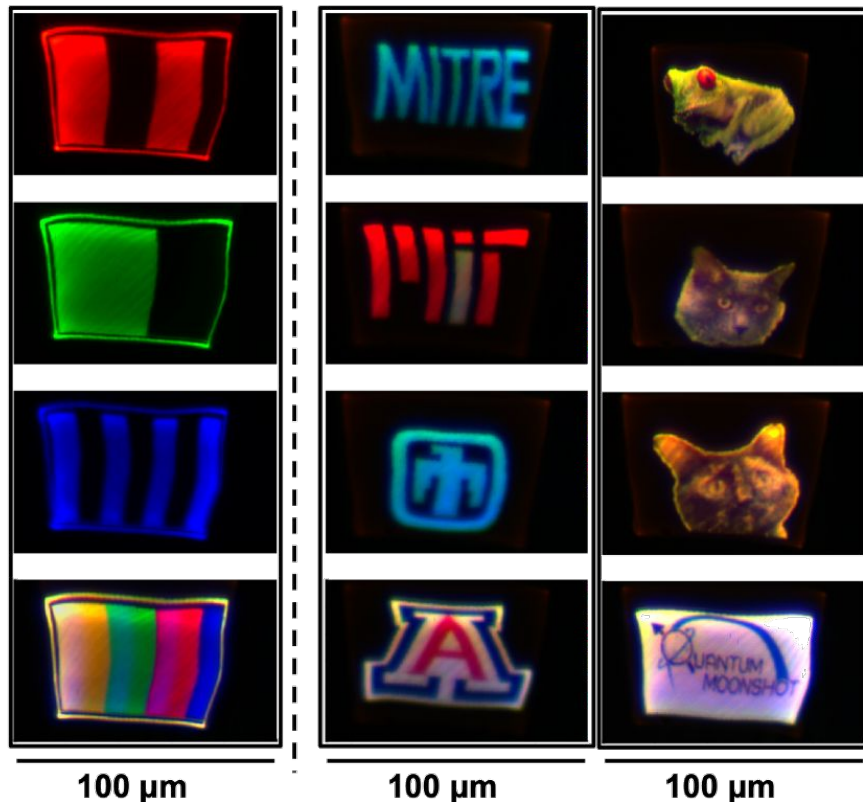
## 3 COMBINED

Arbitrary control



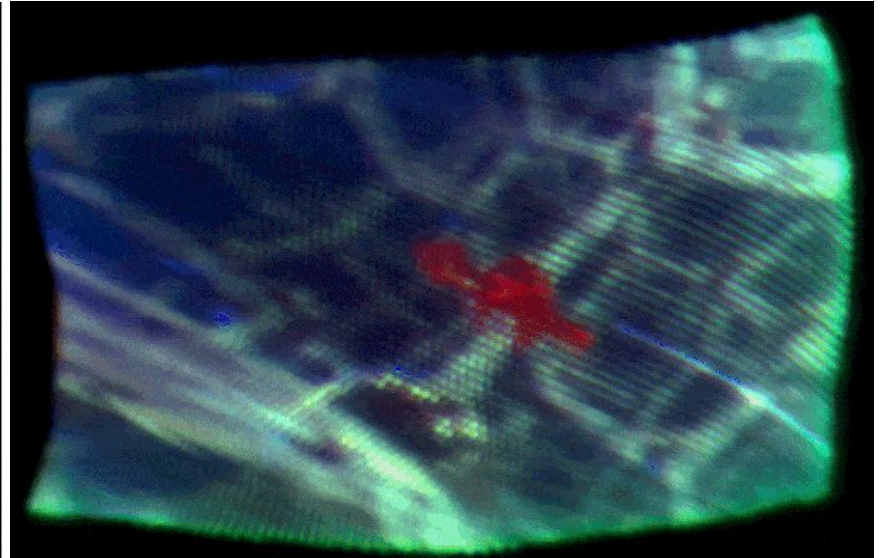
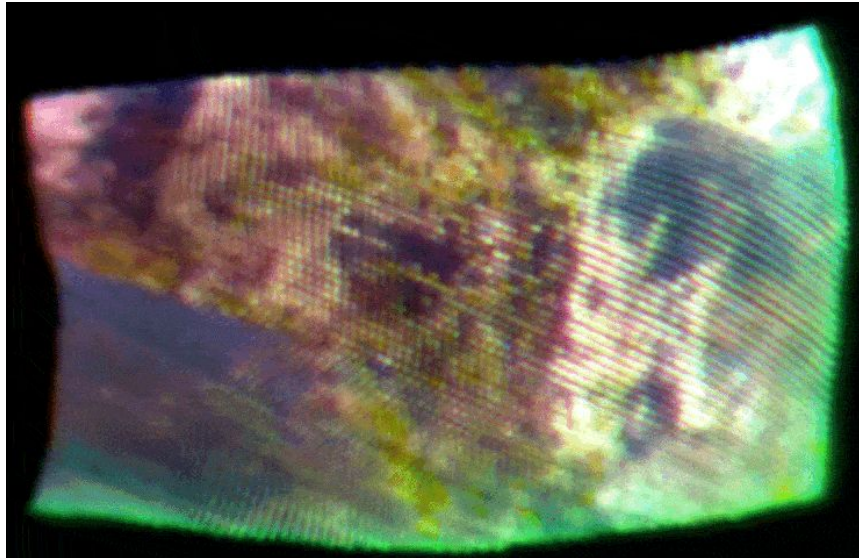
# FULL COLOR IMAGES

23

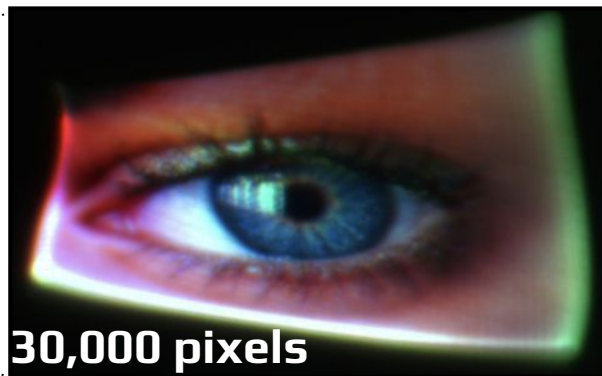
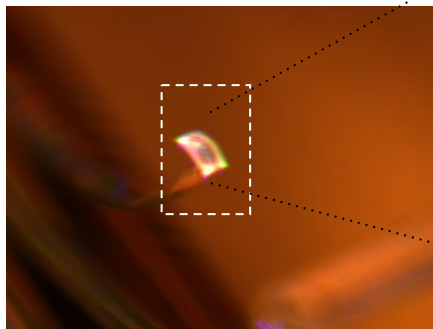


# FULL COLOR VIDEO

24

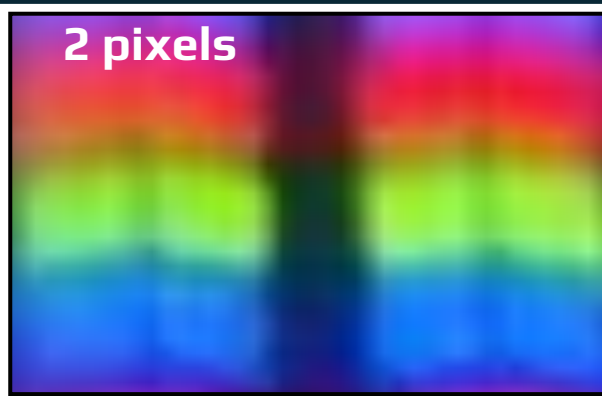
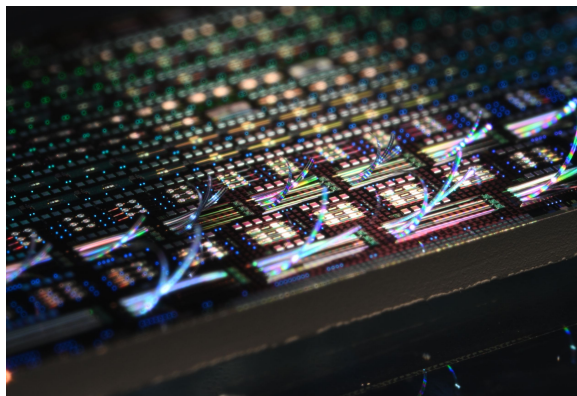




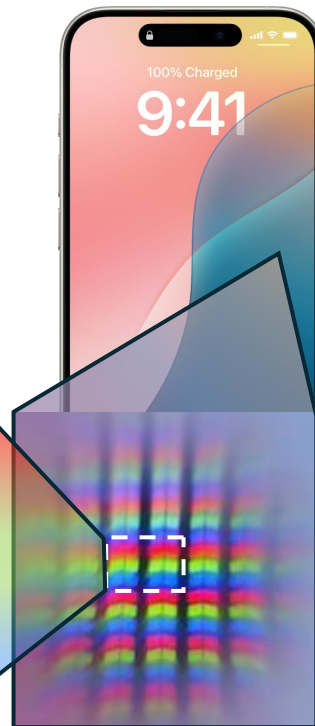


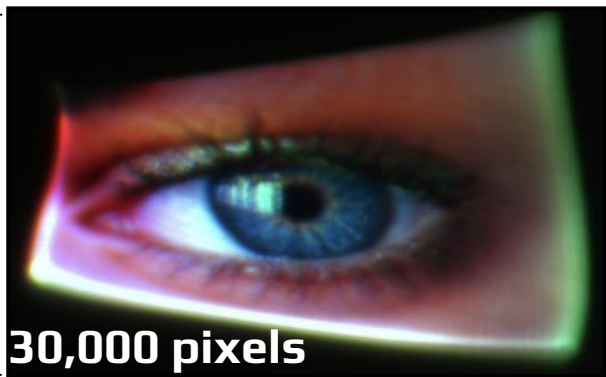
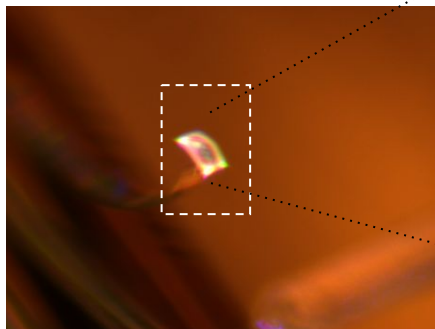
**30,000 pixels**

**in the area of**

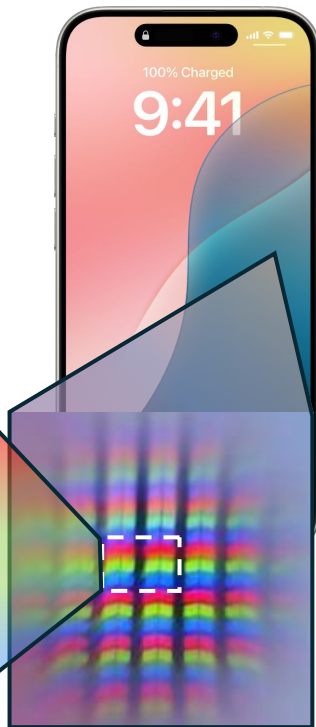
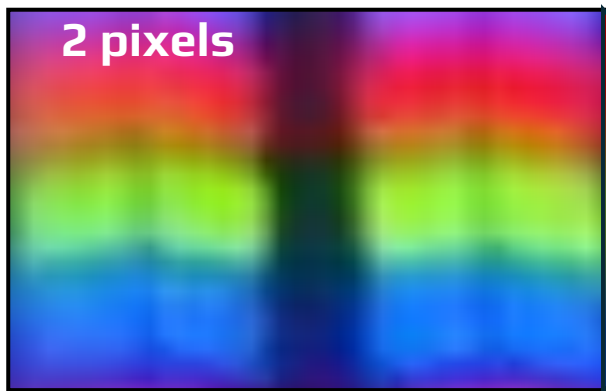
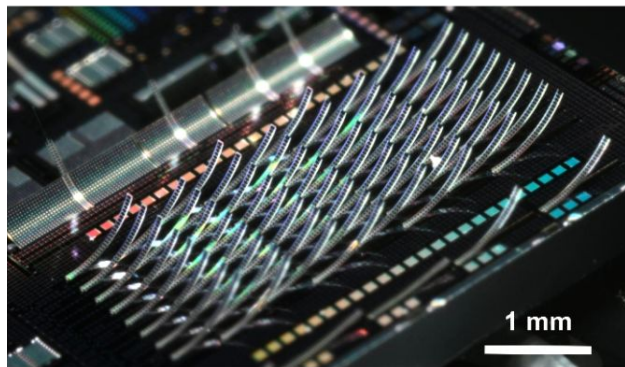


**2 pixels**



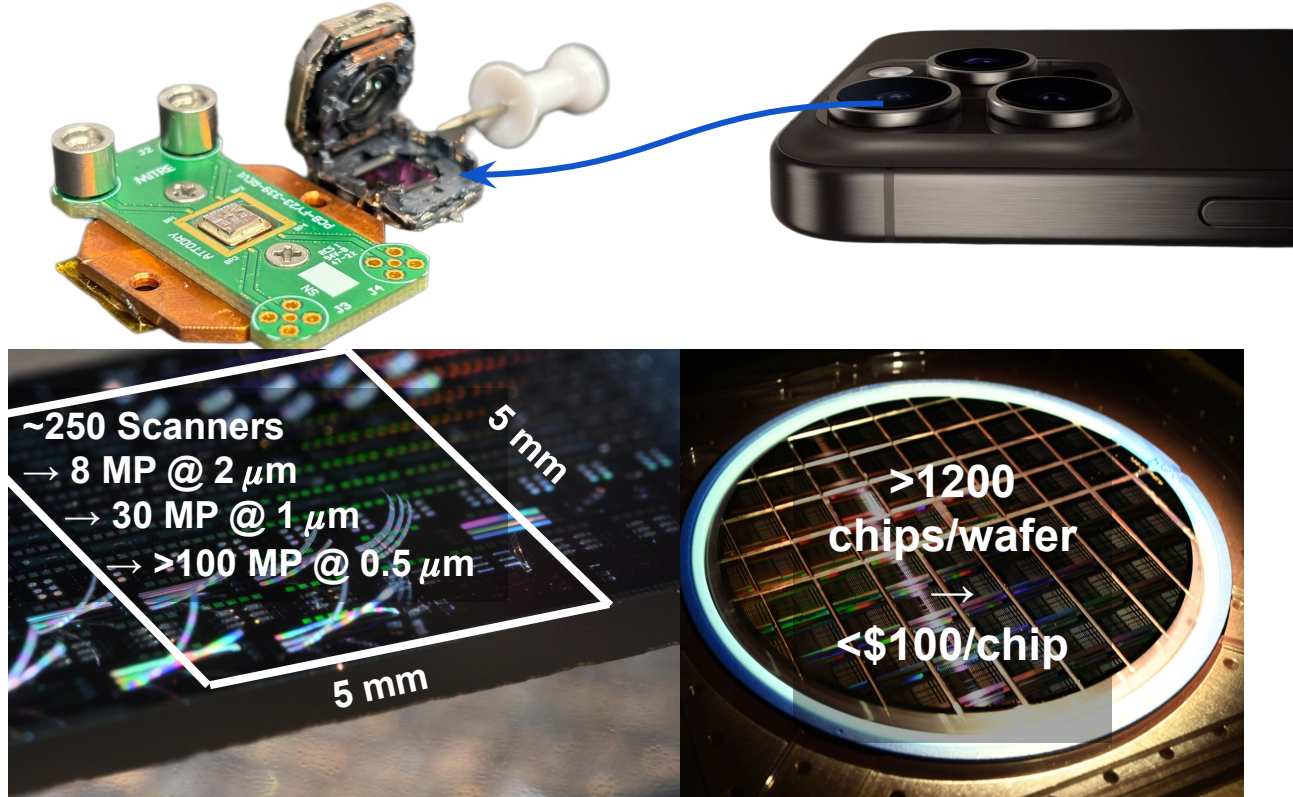


**30,000 pixels**  
**in the area of**



# SWARM: Scanning waveguide AR microdisplay

27





# WHAT'S NEXT: LAB TO DEVICE

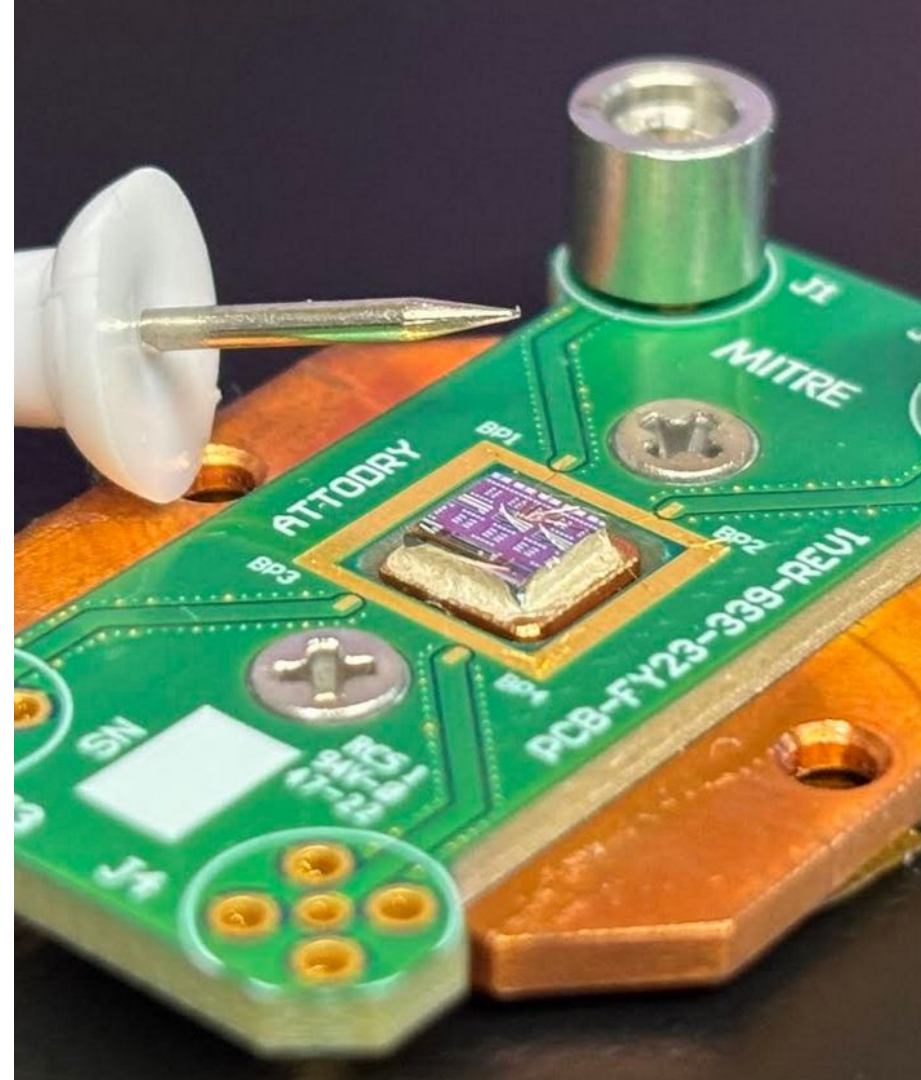
**FABRICATION UNIFORMITY**

**MICROLENS ARRAY DESIGN FOR  
ABERRATION COMPENSATION**

**COUPLING OPTICS INTEGRATION**

**ELECTROMECHANICAL INTEGRATION  
INTO SMALL FORM FACTOR**

**CONTROL & SOFTWARE INTERFACE**





## Deep-Dive #2:

# Verifiable Measurements

# Bidirectional Nonlinear Optical Tomography: Unbiased Characterization of Off- and On-Chip Coupling Efficiencies

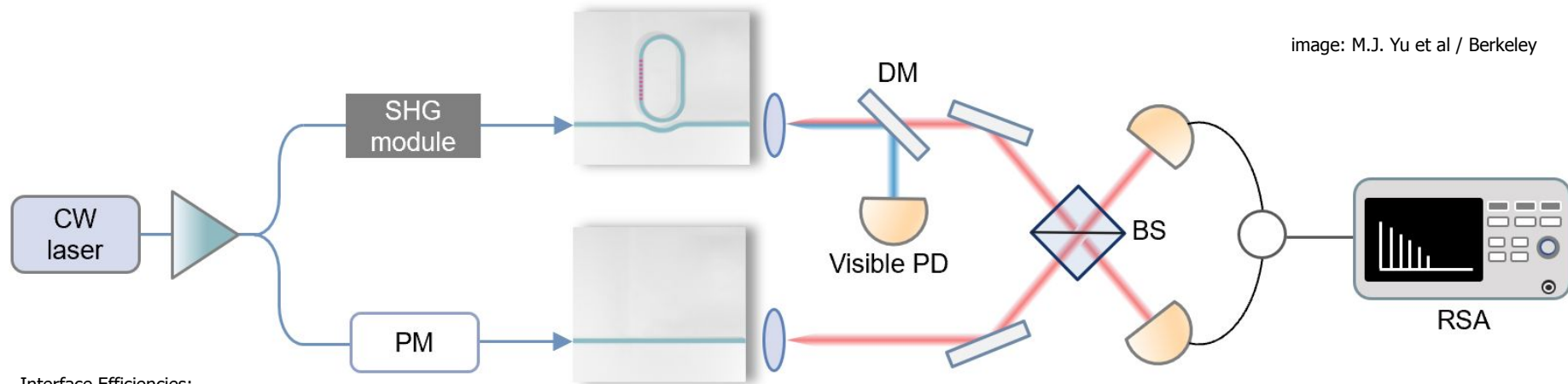
Bo-Han Wu,<sup>1,2,\*</sup> Mahmoud Jalali Mehrabad,<sup>1</sup> and Dirk Englund<sup>1</sup>

<sup>1</sup>*Research Laboratory of Electronics, Massachusetts Institute of Technology, Cambridge, Massachusetts 02139, USA*

<sup>2</sup>*Electrical and Computer Engineering, University of Hawai'i at Mānoa, Honolulu, Hawai'i 96822, USA*

(Dated: October 16, 2025)

# Squeezed light generation and detection



## Interface Efficiencies:

- $\eta_1(2\omega)$ : Input coupling efficiency at pump wavelength ( $2\omega \approx 775$  nm)
- $\eta_2(\omega)$ : Output coupling efficiency at signal wavelength ( $\omega \approx 1550$  nm)

## Cavity Parameters:

- $\kappa c(i)$ : Coupling decay rate for ring  $i$  (Hz)
- $\kappa_i(i)$ : Intrinsic loss rate for ring  $i$  (Hz)
- $\mu(2\omega)$ : Inter-ring coupling rate at  $2\omega$  (Hz)
- $\omega_0$ : Cavity resonance frequency (rad/s)

## Material Properties:

- $n\omega = 2.18$ : Refractive index at 1550 nm
- $n2\omega = 2.14$ : Refractive index at 775 nm
- $d_{eff} = 19.5$  pm/V: Effective nonlinear coefficient

## A1: Single-Mode Operation

- All fields propagate in the fundamental TE mode.
- Scattering to higher-order modes is negligible.
- Justification: Mode overlap calculations indicate greater than 99% fundamental mode content.

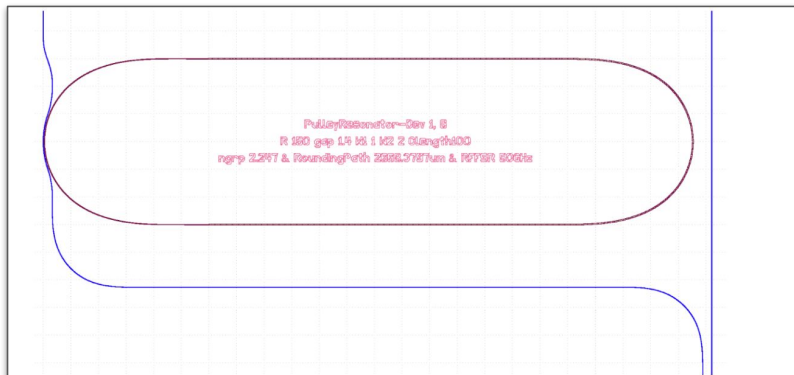
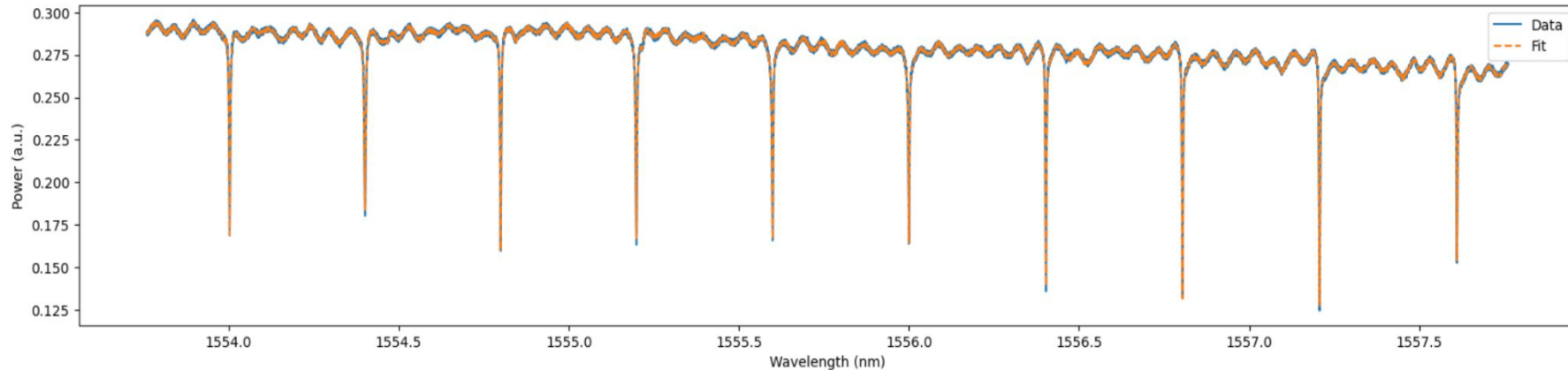
## A2: Lorentzian Resonance

- The cavity transmission exhibits a Lorentzian lineshape, valid for  $Q > 10^4$  (typical for TFLN rings).
- Mathematical Representation:  $T(\omega) = \kappa c^2 / ((\omega - \omega_0)^2 + (\kappa_{tot}/2)^2)$

A3: Time-Invariant Device (not currently the case  $\rightarrow$  experiment upgrades + model upgrades). We want, but can't have: Device parameters ( $\kappa$ ,  $\mu$ ,  $\omega_0$ ) remain constant during measurements;

# Digital twin: fitting the data with ambiguity

- Refined fitting routine give is expressive enough -- but it's not unique.
- 



## Ring

Bending radius = 150  $\mu\text{m}$

Gap = 1.4, 1.2, 1.0, 0.9, 0.8, 0.7  $\mu\text{m}$

Bus wg width = 1  $\mu\text{m}$

Ring wg width = 2  $\mu\text{m}$

Coupling length = 100  $\mu\text{m}$

Ring path length = 2668  $\mu\text{m}$

FSR = 50 GHz

Simulated  $n_{\text{eff}}$  = 1.939147

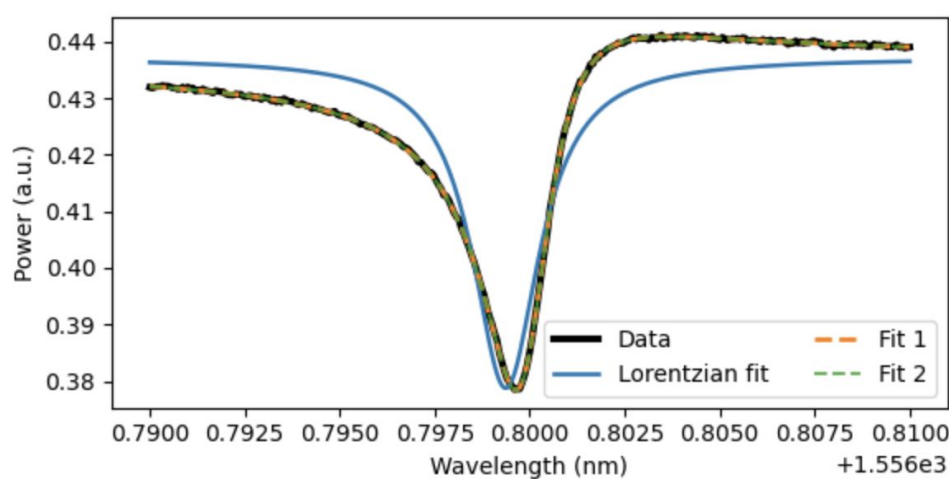
Simulated  $n_g$  = 2.242544

Estimated bus waveguide length (facet to facet) = 9.1 mm

S. Y. Ma / MIT  
Berkeley team  
(measurements)

# Digital twin: fitting the data with ambiguity

- Different parameters can lead to the same fitting curve: ambiguity



fitting includes laser model +  
detector model + linear optics

$$E_{\text{det}}(\omega) = E_{\text{chip}}(\omega) + E_{\text{bg}}(\omega),$$
$$P(\omega) = |E_{\text{det}}(\omega)|^2.$$

Dispersive coupler

$$\kappa(\omega) = \kappa_0 + \kappa_1(\omega - \omega_{\text{ref}})$$

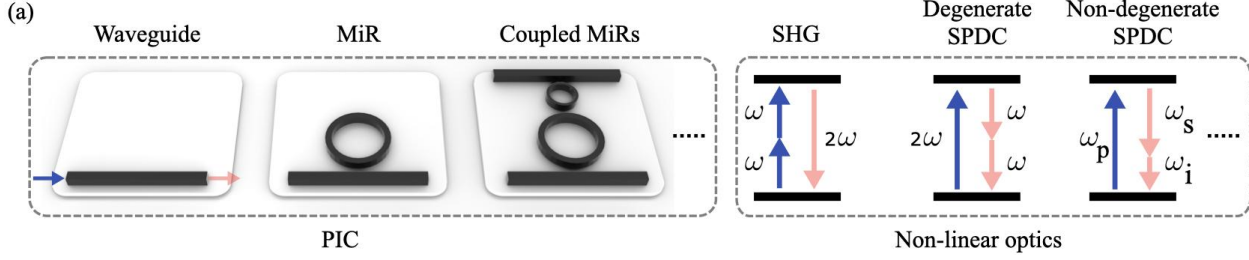
Lorentzian fit: default symmetric fitting.

Fit 1: backscattering  $c = 0.0173$ , minor model  $|E_{\text{bg}}| < 0.001$ .

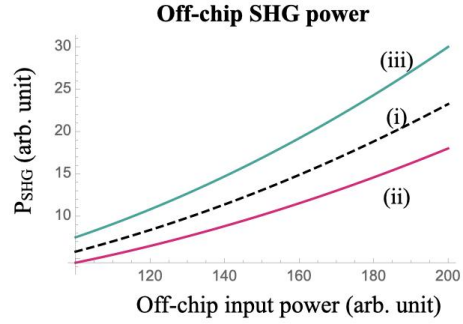
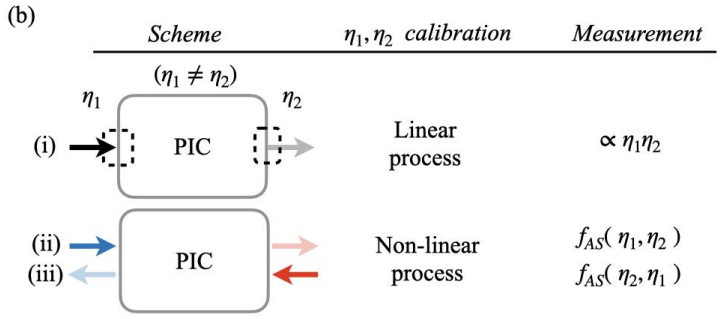
Fit 2: backscattering  $c = 0.001$ , minor model  $|E_{\text{bg}}| \sim 0.008$ , altered  $\kappa \sim 2\%$ .

Cannot uncover ground truth in **one measurement** → Need to lift collinearity with

# Bidirectional nonlinear optical tomography (BNOT)

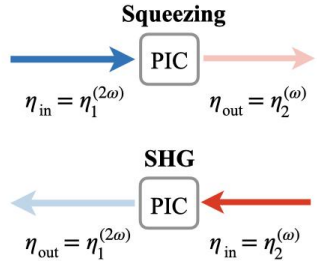
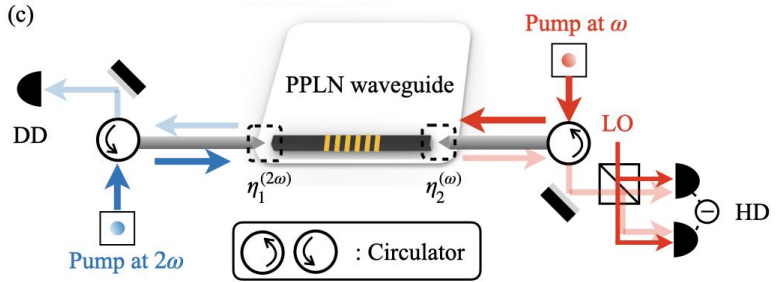


→ A general calibration framework for nonlinear integrated optics.



→ Conv. approach, (i), uses linear process to “**degenerately**” estimate interface efficiencies.

→ BNOT approach, (ii) and (iii), uses nonlinear process to “**non-degenerately**” estimate interface efficiencies.

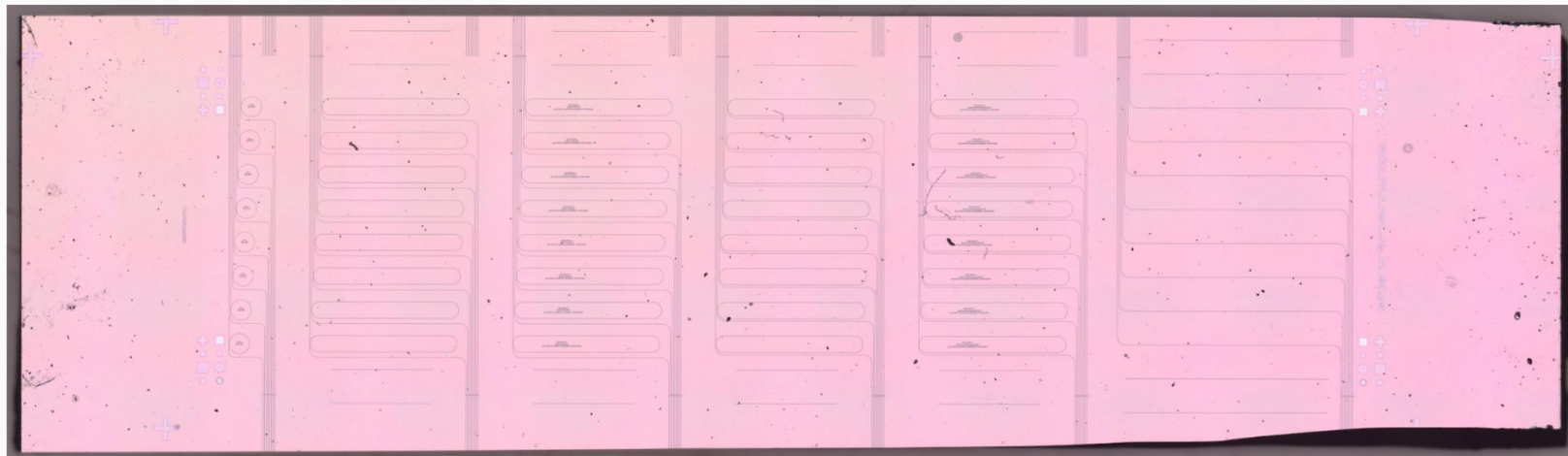


→ Particularly important for strongly squeezed light experiments (i.e., >16 dB).



# Closed-Loop Architecture

**Workflow:** (1) Ingest lab data → (2) Run BNOT → (3) Update twin → (4) Predict performance



M.J. Yu group,  
Berkeley

**Toolchain:** Python-based simulator with pytest validation suite and continuous integration.

# Deep Learning on Wireless Networks:

Matching the Accuracy of Von Neumann Machines below Their Thermodynamic Limits

Sri Krishna Vadlamani, Kfir Sulimany, Zhihui Gao, Tingjun Chen, and Dirk Englund - **arXiv:2504.1775**

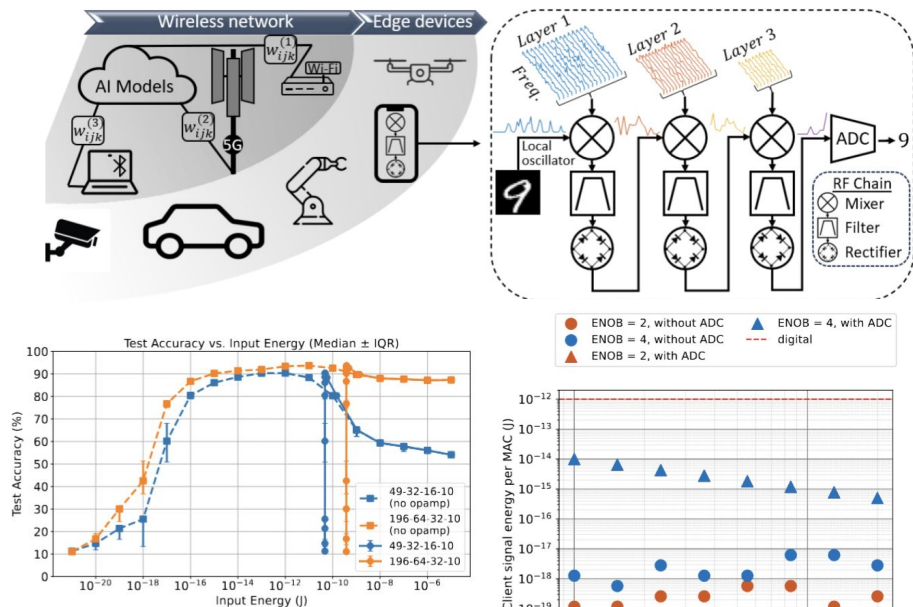
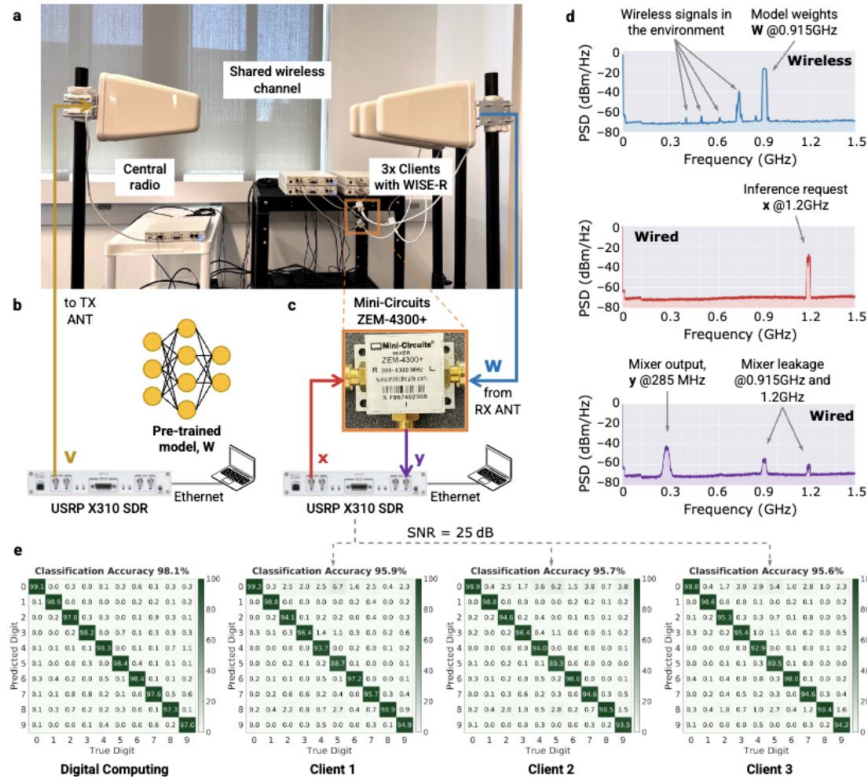


FIG. 4. MNIST classification accuracy of RF analog and digital deep learning. MNIST classification accuracy is presented as a function of the total energy per MAC for digital and analog systems.

FIG. 3. Energy per MAC versus inputsize of the inner product vectors

# Disaggregated Deep Learning via RF Computing at Radio Frequency

Zhihui Gao, Sri Krishna Vadlamani, Kfir Sulimany, Dirk Englund, and Tingjun Chen - **arXiv:2505.09267**



Basic research

Technology transition

Industry, gov't partnerships

Startups

**LIGHTMATTER**

acceleration  
Founded 2017

<https://lightmatter.co/>

matrix PARTNERS | Hewlett Packard Enterprise | Viking | SPARK CAPITAL | NIP Global Partners | Google ventures

**QUNETT**

Quantum Network Technologies, Inc

Quantum communications,  
interconnects, memories

[qunett.com](http://qunett.com)

**QERA**

.. with CUA team  
members Lukin,  
Greiner, Vuletic

Compute the Impossible™

AWS  
**re:Invent**

NOV. 29 - DEC. 3, 2021 | LAS VEGAS, NV

CELEBRATING 10 YEARS OF REINVENT

THE 22 STARTUPS TO WATCH  
IN BOSTON IN 2022

MIT  
Technology  
Review

COMPUTING  
Mathematicians are deploying algorithms to  
stop gerrymandering

This new startup has built a record-breaking  
256-qubit quantum computer

**DUST IDENTITY**

secure digital

Mission:  
Protect the  
hardware of  
critical assets

STARTUP  
KLEINER PERKINS | AIRBUS VENTURES | CASTLE ISLAND | angular ventures

**LIGHTIUM**

CRRAFTING LIGHT SHAPING THE FUTURE

PRODUCTION-GRADE  
PHOTONIC FOUNDRY FOR  
THIN-FILM LITHIUM NIOBATE

**Axiomatic AI**

First-Principles Engineering

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Home Team News

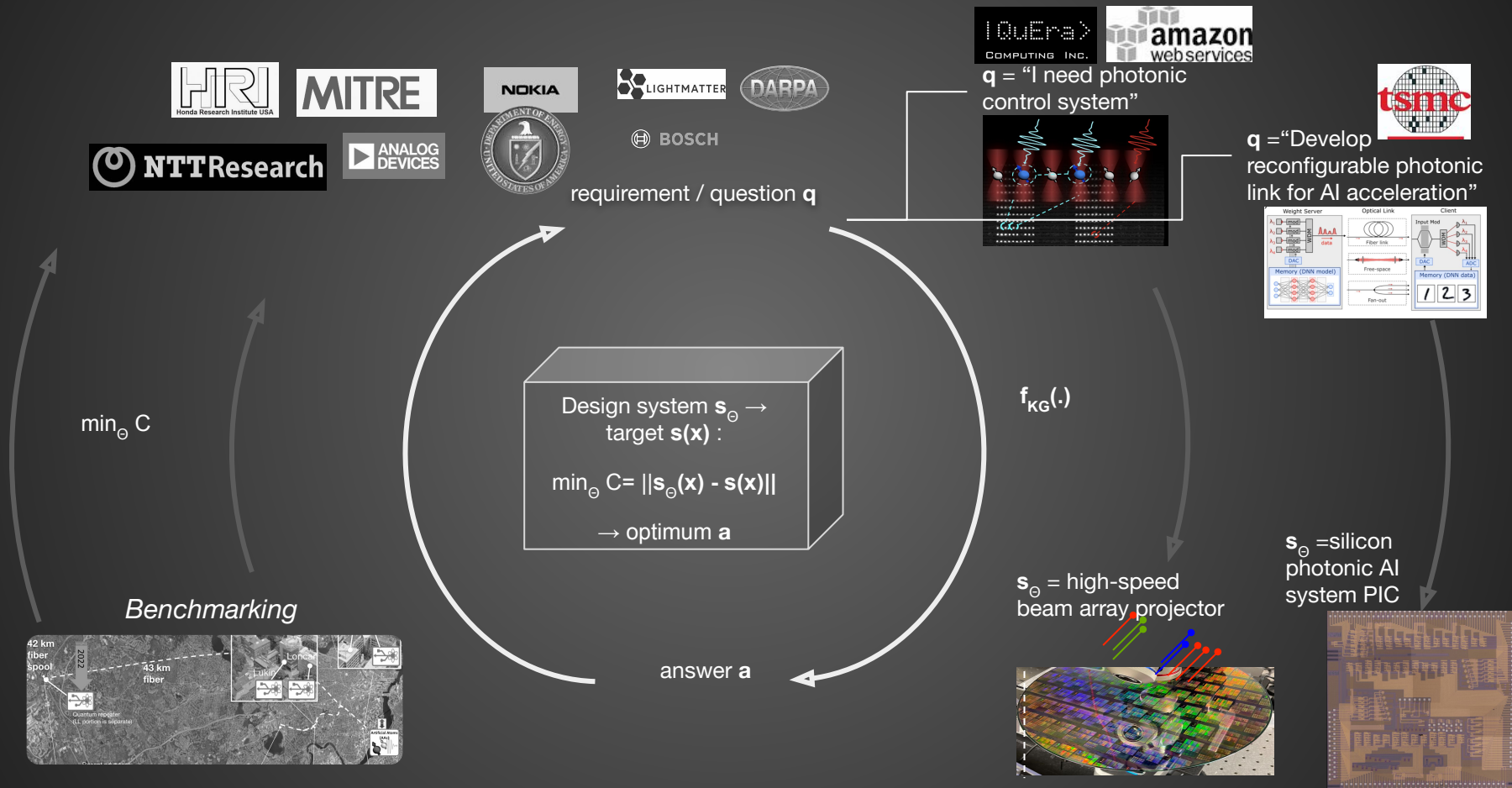
Zaijun Chen  
Mengjie Yu  
Ryan Hamerly

Startup hiring (<https://netpreme.com/>)

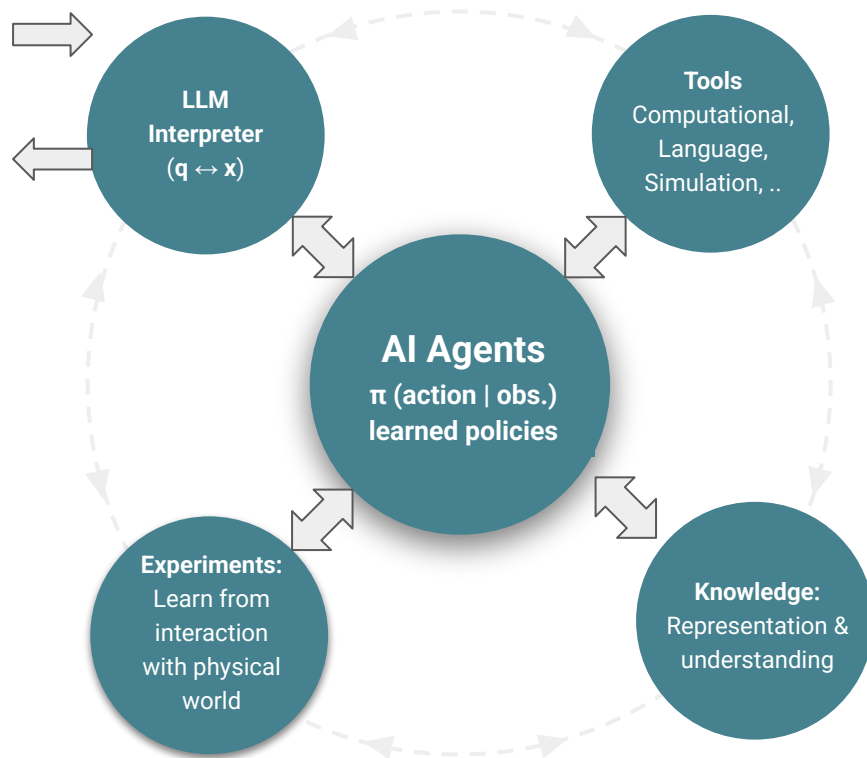
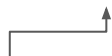
**Netpreme**

Dr. Zhizhen Zhong

# From question to ~~solution~~ question to...

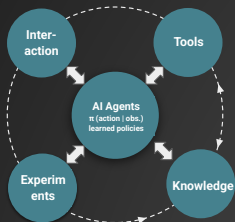


# What “generative design” may look like





## Example 1: math-grounded reasoning



## The Verification Gap

### OpenAI's GPT5

ChatGPT 5 >

We are solving the equation:

$$5.9 = x + 5.11$$

**Step 1: Isolate  $x$**

Subtract 5.11 from both sides:

$$x = 5.9 - 5.11$$

**Step 2: Perform the subtraction carefully**

$$5.90 - 5.11 = 0.79 - 0.00 - 0.21 = -0.21$$

(We can think of  $5.90 - 5.11$  as subtracting 5.11 from 5.90 directly, which equals -0.21.)

**Final Answer:**

$$x = -0.21$$

So the solution is:

$$x = -0.21$$



Ask anything



Leading LLM error rates of  $10^{-2}$  are much too high for science, math, engineering

Claude Shannon, in his seminal work [19] introduced the concept of diffusion properties for any cryptosystem. The diffusion property is a linear layer, often represented by a permutation, that provides a significant alteration in the strength of the diffusion layer. The optimal branch number is achieved when the branch number is 2.

$$\min \left\{ h(M, x) \mid \right.$$

Note that the right-hand side of (4) is always greater than or equal to the left-hand side of (4). Therefore, if we include this extra term in (3), it will not affect

Note that the right-hand side of (4) is always greater than or equal to the left-hand side of (4). Therefore, if we include this extra term in (3), it will not affect

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1767 -- KEY SORRIES: THE ORIGINAL PROOF USES MINIMUMS OF EMPTY FINSETS, WHICH ARE NOT DEFINED
1768 have h_constrained_low_nonempty : { { x ∈ (@low_weight_vectors p q n _ _) | wH (M.mulVec x) ≤ (n + 1) / 2 } }.Nonempty := by sorry
1769 have h_first_set_nonempty : { y ∈ (@high_weight_vectors p q n _ _) | wH (M.mulVec y) ≤ (n + 1) / 2 }.Nonempty := by sorry
1770 have h_second_set_nonempty : { y ∈ (@high_weight_vectors p q n _ _) | wH (M.mulVec y) > (n + 1) / 2 }.Nonempty := by sorry

```

>cs>arXiv:2510.12787v2 (2025)

# Concrete scenario: VVUQ of patent (100+ equations)

U.S. Patent Jul. 21, 2009 Sheet 9 of 12 US 7,564,534 B2

(12) United States Patent  
Den Boef et al.

(10) Patent No.: US 7,564,534 B2  
(45) Date of Patent: \*Jul. 21, 2009

US 7,564,534 B2

11  
angle of 40 mrad for  $\lambda=633$  nm. To measure such a low spatial frequency, the angular size of the illumination beam must be limited to a diameter of about 40 mrad.  
In the alignment system 10, the illumination spot is circularly polarized to enable illuminating and detection light to be separated with the aid of polarizing beam splitter 17 and a 0-order quarter wave plate 18 as shown in FIG. 3.

For coarse gratings with a pitch much greater than the wavelength of the illumination beam, the choice of polarization is not very important. However, where the marker pitch is of the same order as the wavelength, the diffraction efficiency depends on the polarization alignment marker can act as a polarization component. Focused light is sub-wavelength light there is always a chance very low for one particular light contains two orthogonal 90° phase shift) so there is efficiently diffract the light.

In order to suppress spurious apply a minor tilt to the polarizer quarter wave plate 18. The tilt to minimize aberrations this course, it is also possible to design of the objective lens. The interferometer produces (virtual) images of the pupa frequency. The total optical field original field plus a 180° rotation in the pupil plane is:

$$M(x_0, y_0, z_0) = E_0(x_0, y_0, z_0) + E_0^*(x_0, y_0, z_0) \quad (1)$$

If two detectors 15 with a width  $2\Delta k$  are placed at positions  $k_0$  and  $-k_0$  in the pupil plane 14, the optical powers  $P_1$  and  $P_2$  captured by these detectors are given by:

$$P_1(k_0) = \int_{-k_0-\Delta k}^{-k_0+\Delta k} |E_0(k)|^2 dk + \int_{-k_0-\Delta k}^{-k_0+\Delta k} E_0(k) E_0^*(k) dk + \int_{-k_0-\Delta k}^{-k_0+\Delta k} E_0(k) E_0^*(k) dk \quad (2)$$

$$P_2(k_0) = \int_{k_0-\Delta k}^{k_0+\Delta k} |E_0(k)|^2 dk + \int_{k_0-\Delta k}^{k_0+\Delta k} E_0(k) E_0^*(k) dk + \int_{k_0-\Delta k}^{k_0+\Delta k} E_0(k) E_0^*(k) dk \quad (3)$$

FIG. 5 shows the signal formation graphically. Because of the mirror operation, the horizontally hatched areas overlap and interfere and the diagonally hatched areas overlap and interfere. The phase difference between the two fields contains the position information.

The two images of the pupil are orthogonally and linearly polarized and interference between them is therefore not visible in the form of intensity variations (fringes). In order to translate phase variations in intensity variations, the two images of the pupil must have the same polarization which is realized with a polarizing optical element, which may be a dichroic sheet polarizer, a regular polarizing beam splitter based on a multi-layer coating, or a birefringent beam splitter such as a Savart plate, a Wollaston Prism, a Glan-Thompson beam splitter or a "wire grid" polarizer.

12  
Dichroic sheet polarizers are not preferred because of their limited optical quality and they are often less effective in the near-IR region. Moreover, these sheet polarizers throw away 50% of the photons. A multi-layer beam splitter is far better but the wavelength range over which a good extinction ratio is achieved may be limited. Birefringent beam-splitters have excellent extinction ratios over a large wavelength range but the birefringence may lead to temperature drift since the birefringence is temperature dependent.  
If a beam splitter is used as polarizer 19, the field incident on it has a Jones vector:

$$I_1(k) = \frac{1}{2} |E(k)|^2 + \frac{1}{2} |E(-k)|^2 + |E(k)| |E(-k)| \cos(\varphi(k) - \varphi(-k)); \quad (5)$$

and

$$I_2(k) = \frac{1}{2} |E(k)|^2 + \frac{1}{2} |E(-k)|^2 + |E(k)| |E(-k)| \cos(\varphi(k) - \varphi(-k)). \quad (6)$$

the total intensity equals the intensity that is incident on the beam splitter. Thus, both branches contain position information and can be used for alignment. This means that it is possible to use one branch for x-position detection and the other for y-position detection, allowing use of rectangular aperture stops to avoid product cross-talk. Alternatively, one branch can be used with a small aperture stop for fine alignment and the other branch with a large aperture stop for capturing. A further alternative is to use one branch for one set of wavelengths and the other branch for another set of wavelengths.

Alignment markers are often placed in the scribe lane very close to product structures which may lead to product cross-talk: light scattered by the product influences the alignment signal. Product cross-talk can be strongly attenuated by using a sufficiently small illumination beam. However, a small illumination beam is not preferred for various reasons. With a small illumination beam, the stability of the position of the illumination spot becomes more critical. For example, in the extreme case of a scanning spot, drift in the illumination spot results directly in alignment position drift. Also, capturing becomes more critical since there is a greater chance that the marker is very poorly illuminated after the substrate W is loaded on the substrate table WT. Finally, a greater illumination NA is needed which makes the detection of coarse gratings more demanding.

For these reasons it is desirable to use a large illumination spot, for example with a  $1/e^2$  width of roughly three times the maximum marker diameter. The consequences of such a large spot are that product structures are illuminated and that the optical power on the marker decreases. However, the latter item is not a serious problem since a sufficiently powerful light source can be provided.

The issue of product cross-talk can be solved with aperture stops that are placed at an intermediate image of the marker, as shown in FIG. 9. Since the alignment system 10 requires no

## AXIOMATIC FULL EQUATION CHECK

1) Ingest  
Patent

2) Extract  
Formulas

3) Symbolic Verification Engine  
(loop until clean)

Verification

✓ Equation 1: CORRECT

Cross-Check

✗ Equation 5-6 Line 2: ERROR

Errors?

Yes

Error Report

Published:

$$I_r(k) = 1/4 |E(k)|^2 + 1/4 |E(-k)|^2 + |E(k)| |E(-k)| \cos(\varphi(k) - \varphi(-k))$$

Should be:

$$I_r(k) = 1/4 |E(k)|^2 + 1/4 |E(-k)|^2 - |E(k)| |E(-k)| \cos(\varphi(k) - \varphi(-k))$$

Issue: Wrong sign (+ vs -)

No

UPSHOT:

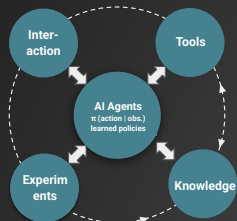
• Avoid legal challenge to patent  
• Detected in ~5 min via parallel orchestration

Mathematical Validation

Residual = 0

|Line1 - Line2| = 0.0

∴ Equations are equivalent



# AX-Prover: A DEEP REASONING AGENTIC FRAMEWORK

Example of “basic” math (abstract algebra)

For example, a competition problem may ask to determine all positive integers  $a, b$  such that

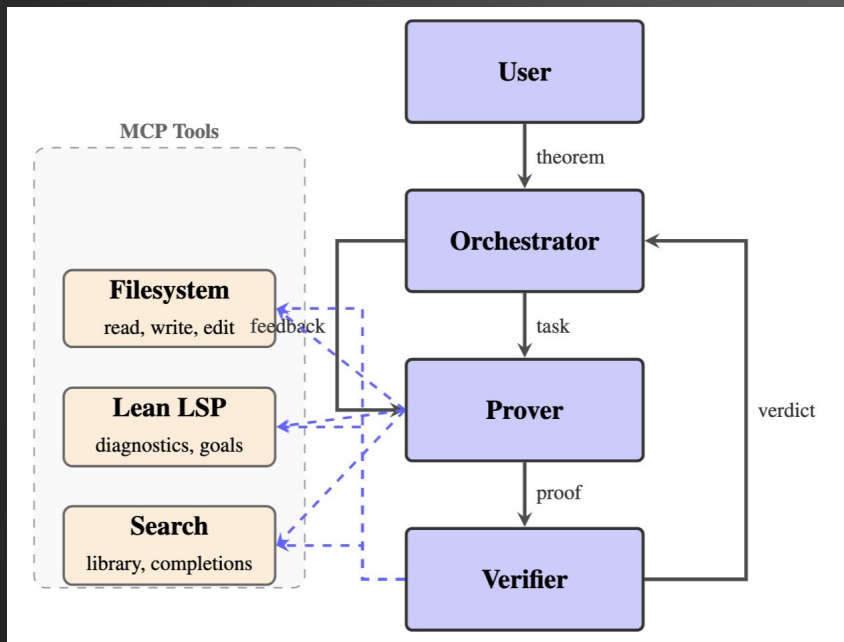
$$\frac{a^2 + b^2}{ab + 1} \in \mathbb{Z},$$

Example cryptography proof

**Theorem 1.** *The branch number of an invertible matrix  $M \in M_n(\mathbb{F}_q)$  is given as*

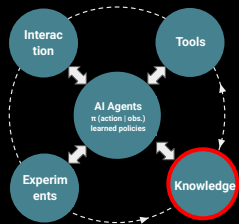
$$B(M) = \min \left\{ \min \{ h(M, x), h(M^{-1}, x) \} \mid x \in \mathbb{F}_q^n, 1 \leq w_h(x) \leq \left\lfloor \frac{n+1}{2} \right\rfloor \right\},$$

where  $h(M, x) = w_h(x) + w_h(Mx)$ .



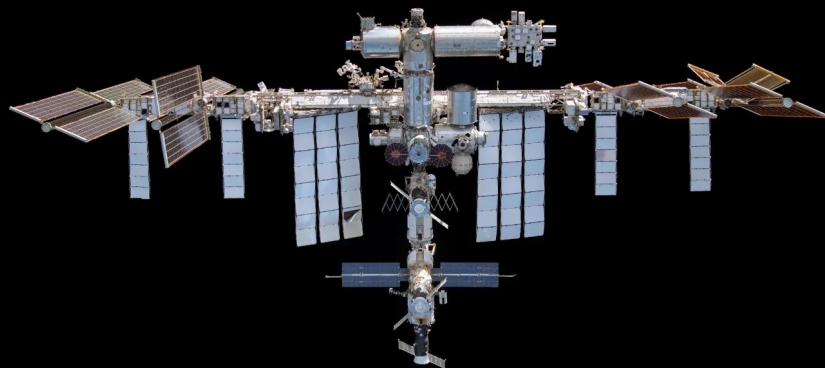
Dataset	Subset	Ax-Prover (pass@1)	Sonnet (pass@1)	DS-Prover (pass@1)	Kimina <sup>†</sup>
NuminaMath	solved-K	81%	7%	48%	100%
	solved-H	47%	8%	14%	0%
	unsolved	26%	1%	18%	0%
	total	51%	5%	28%	31%
AbstractAlgebra	easy	72%	10%	26%	12%
	intermediate	56%	6%	22%	14%
	total	64%	8%	24%	13%
QuantumTheorems	easy	100%	54%	88%	72%
	intermediate	92%	18%	48%	34%
	total	96%	40%	61%	57%



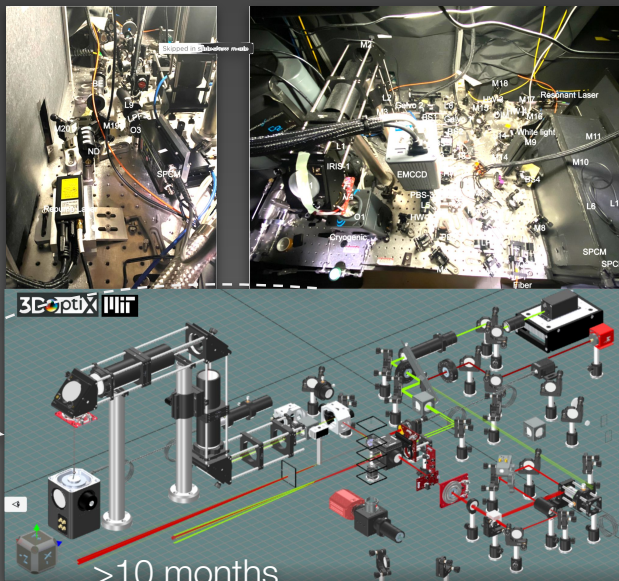


# The Knowledge (Ingress) Gap

understand, model



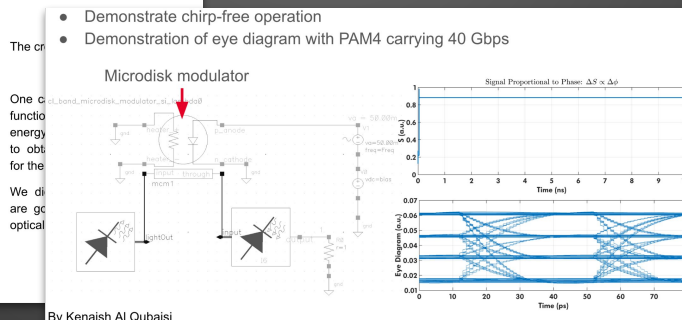
control, refine



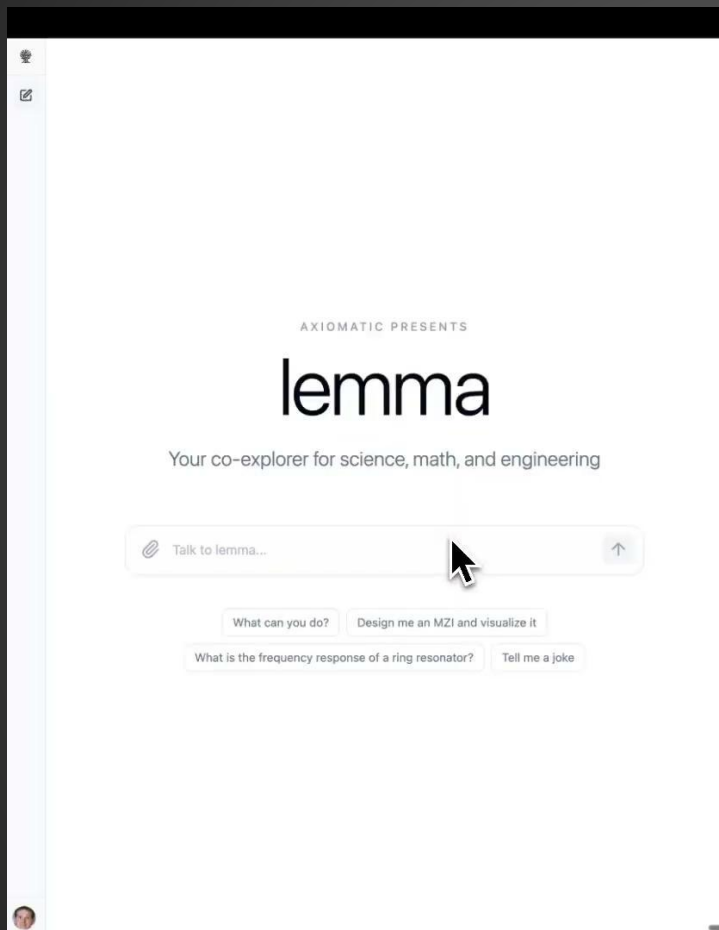
MIT postdoc: "Ansys is state of art but building models containing quantum physics was impossible.. [...] I ended up instead using python, then pytorch, .. and maybe eventually connect with to Ansys, Synopsis tools

[illegible]

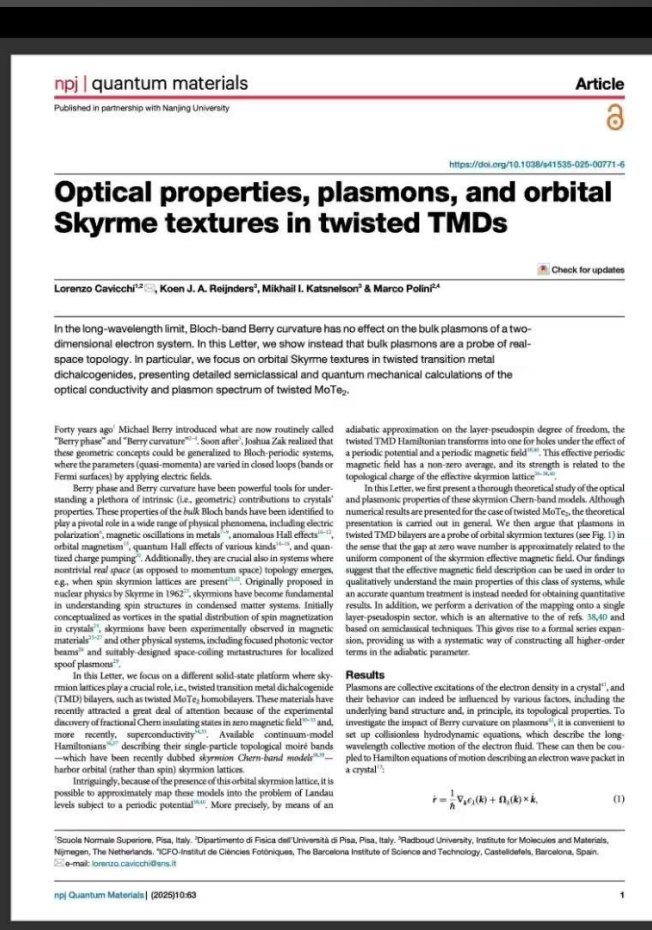
MIT postdoc : “ I didn’t know about digital twin modeling before joining this project, i wish they’d teach that in grad school”



# Example 1: Reading comprehension



The screenshot shows the 'lemma' AI interface. At the top, it says 'AXIOMATIC PRESENTS lemma'. Below this is the tagline 'Your co-explorer for science, math, and engineering'. There is a search bar with the placeholder text 'Talk to lemma...'. Below the search bar are three buttons: 'What can you do?', 'Design me an MZI and visualize it', and 'What is the frequency response of a ring resonator?'. A mouse cursor is hovering over the search bar.



The screenshot shows the first page of a scientific article in npj Quantum Materials. The article title is 'Optical properties, plasmons, and orbital Skyrme textures in twisted TMDs'. The authors are Lorenzo Cavicchi, Koen J. A. Reijnders, Mikhail I. Katnelson, and Marco Polini. The article is published in partnership with Nanjing University. The abstract discusses the long-wavelength limit, Bloch-band Berry curvature, and the bulk plasmons of a two-dimensional electron system. The article is available for free access.

npj | quantum materials  
Published in partnership with Nanjing University

Article

<https://doi.org/10.1038/s41535-025-00771-6>

## Optical properties, plasmons, and orbital Skyrme textures in twisted TMDs

Check for updates

Lorenzo Cavicchi<sup>1,2,✉</sup>, Koen J. A. Reijnders<sup>1</sup>, Mikhail I. Katnelson<sup>3</sup> & Marco Polini<sup>2,4</sup>

In the long-wavelength limit, Bloch-band Berry curvature has no effect on the bulk plasmons of a two-dimensional electron system. In this Letter, we show instead that bulk plasmons are a probe of real-space topology. In particular, we focus on orbital Skyrme textures in twisted transition metal dichalcogenides, presenting detailed semiclassical and quantum mechanical calculations of the optical conductivity and plasmon spectrum of twisted MoTe<sub>2</sub>.

Forty years ago<sup>1</sup> Michael Berry introduced what are now routinely called “Berry phase” and “Berry curvature”<sup>2–5</sup>. Soon after, Joshua Zak realized that these geometric concepts could be generalized to Bloch-periodic systems, where the parameters (quasi-momenta) are varied in closed loops (bands or Fermi surfaces) by applying electric fields.

Berry phase and Berry curvature have been powerful tools for understanding a plethora of intrinsic (i.e., geometric) contributions to crystals’ properties. These properties of the bulk Bloch bands have been identified to play a pivotal role in a wide range of physical phenomena, including electric polarization<sup>6</sup>, magnetic oscillations in metals<sup>7</sup>, anomalous Hall effects<sup>8–11</sup>, orbital magnetism<sup>12</sup>, quantum Hall effects of various kinds<sup>13–15</sup>, and quantized charge pumping<sup>16</sup>. Additionally, they are crucial also in systems where nontrivial real space (as opposed to momentum space) topology emerges, e.g., when spin skyrmion lattices are present<sup>17,18</sup>. Originally proposed in nuclear physics by Skyrme in 1962<sup>19</sup>, skyrmions have become fundamental in understanding spin structures in condensed matter systems. Initially conceptualized as vortices in the spatial distribution of spin magnetization in crystals<sup>20</sup>, skyrmions have been experimentally observed in magnetic materials<sup>21,22</sup> and other physical systems, including focused photonic vector beams<sup>23</sup> and suitably designed space-coiling metastructures for localized spoof plasmons<sup>24</sup>.

In this Letter, we focus on a different solid-state platform where skyrmion lattices play a crucial role, i.e., twisted transition metal dichalcogenide (TMD) bilayers, such as twisted MoTe<sub>2</sub> homobilayers. These materials have recently attracted a great deal of attention because of the experimental discovery of fractional Chern insulating states in zero magnetic field<sup>25–28</sup> and, more recently, superconductivity<sup>29,30</sup>. Available continuum-model Hamiltonians<sup>31</sup> describing their single-particle topological moiré bands—which have been recently dubbed skyrmion Chern-band modes<sup>32–34</sup>—harbor orbital (rather than spin) skyrmion lattices.

Interestingly, because of the presence of this orbital skyrmion lattice, it is possible to approximately map these models into the problem of Landau levels subject to a periodic potential<sup>35–37</sup>. More precisely, by means of an adiabatic approximation on the layer-pseudospin degree of freedom, the twisted TMD Hamiltonian transforms into one for holes under the effect of a periodic potential and a non-zero average, and its strength is related to the topological charge of the effective skyrmion lattice<sup>38–40</sup>.

In this Letter, we first present a thorough theoretical study of the optical and plasmonic properties of these skyrmion Chern-band modes. Although numerical results are presented for the case of twisted MoTe<sub>2</sub>, the theoretical presentation is carried out in general. We then argue that plasmons in twisted TMD bilayers are a probe of orbital skyrmion textures (see Fig. 1) in the sense that the gap at zero wave number is approximately related to the uniform component of the skyrmion effective magnetic field. Our findings suggest that the effective magnetic field description can be used in order to qualitatively understand the main properties of this class of systems, while an accurate quantum treatment is instead needed for obtaining quantitative results. In addition, we perform a derivation of the mapping onto a single layer pseudospin sector, which is an alternative to the use of refs. 38,40 and based on semiclassical techniques. This gives rise to a formal series expansion, providing us with a systematic way of constructing all higher-order terms in the adiabatic parameter.

### Results

Plasmons are collective excitations of the electron density in a crystal<sup>41</sup>, and their behavior can indeed be influenced by various factors, including the underlying band structure and, in principle, its topological properties. To investigate the impact of Berry curvature on plasmons<sup>42</sup>, it is convenient to set up collisionless hydrodynamic equations, which describe the long-wavelength collective motion of the electron fluid. These can then be coupled to Hamilton equations of motion describing an electron wave packet in a crystal<sup>43</sup>:

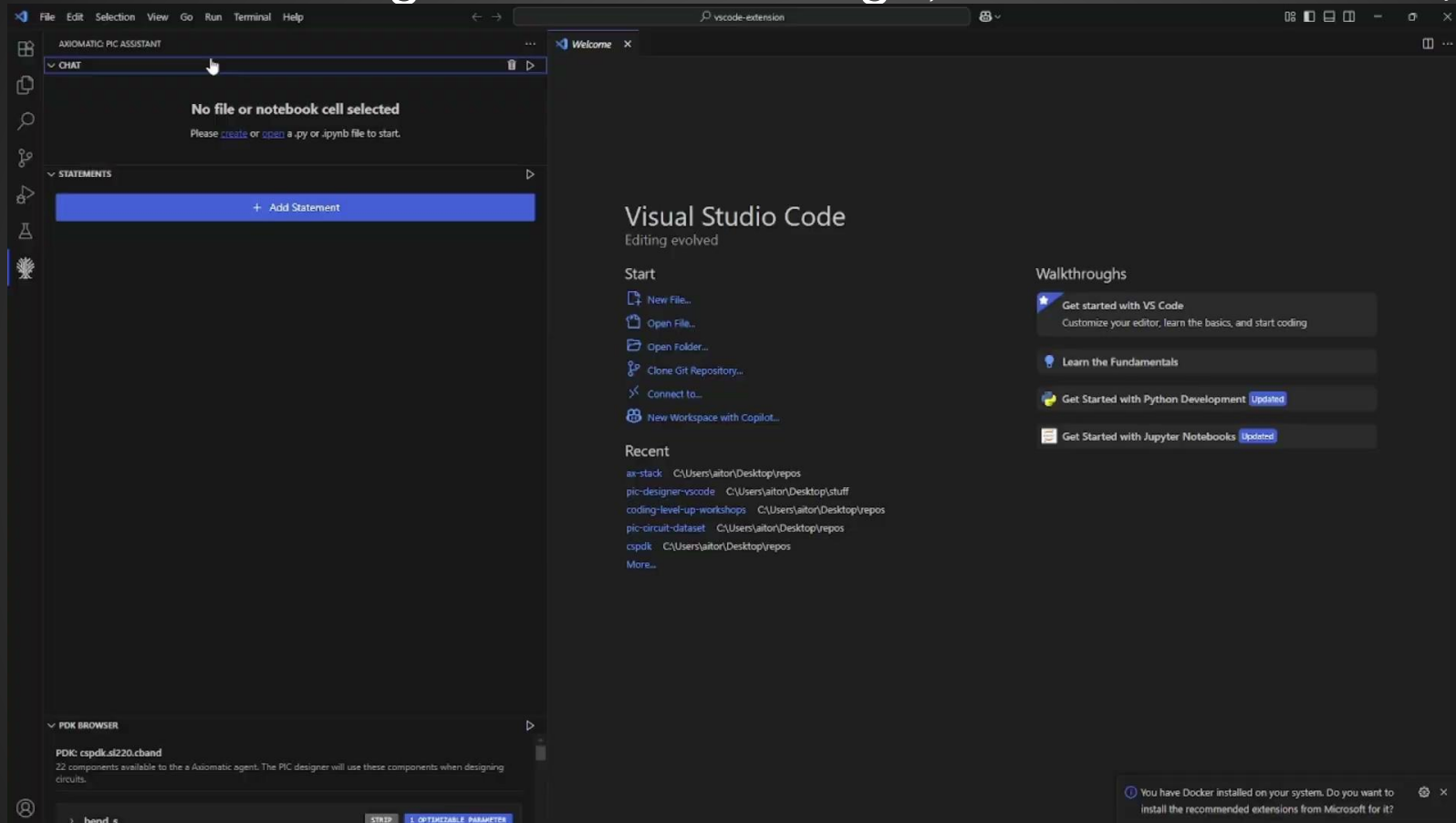
$$\dot{\mathbf{r}} = \frac{1}{\hbar} \nabla_{\mathbf{k}} \epsilon_{\mathbf{k}}(\mathbf{k}) + \Omega_{\mathbf{k}}(\mathbf{k}) \times \hat{\mathbf{k}}, \quad (1)$$

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npj Quantum Materials | (2025)10:63

# Photonic integrated circuit design, automated

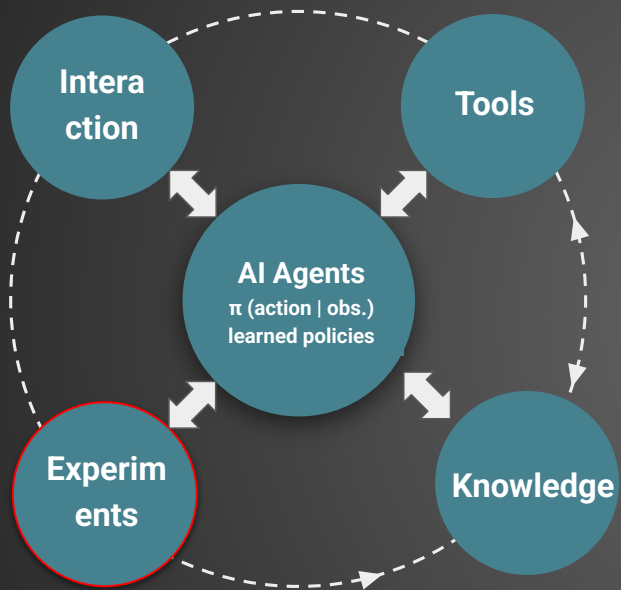
U. Toronto - Axiomatic\_AI -  
GDSFactory - MIT



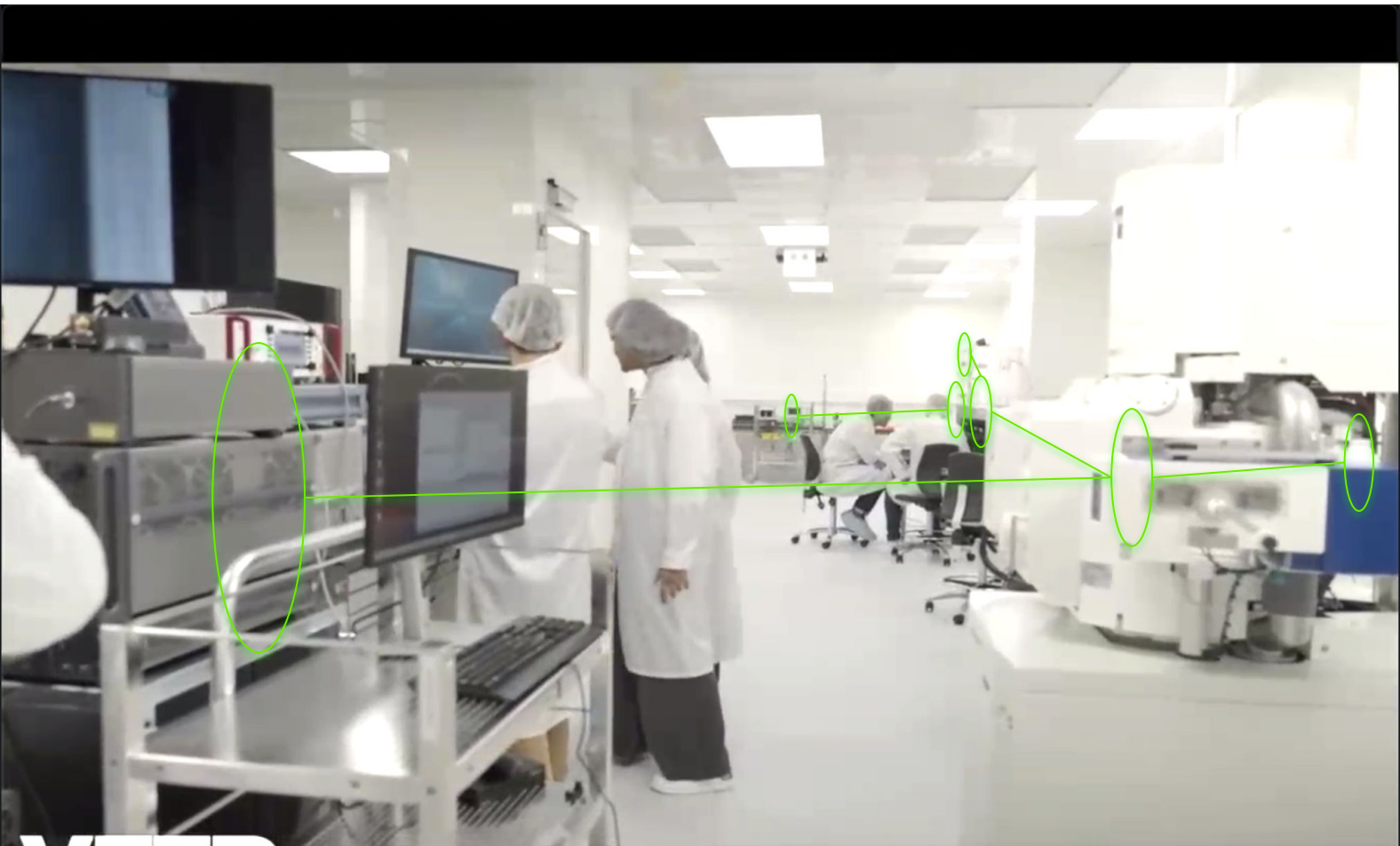
**Opensource:** <https://github.com/JPPhotonics/PhIDO-Release>

**A Sharma**, V Ansari, Y Fu, R Iyer, J Matres, T Tamas, O Akdeniz, D E , J Poon, OFC 2024; to be published;





## 4. Experiments



# Digital twins to make the physical world intelligible

- Infinite space for compiling computing into physics and control.
- Math-grounded AI can help us explore this space of deep computational design

“To reach true AI, we need to build machines that learn models of the world in a self-supervised manner.”

Y. LeCun, “A Path Towards Autonomous Machine Intelligence” (2022)

The Verification Principle:

An AI system can create and maintain knowledge only to the extent that it can verify that knowledge itself.

Rich Sutton, “Verification: The Key to AI” (2002)